CCE SAMPLE QUESTION PAPER 1

FIRST TERM (SA-I)

MATHEMATICS

(With Solutions)

CLASS X

Time Allowed : 3 to 3% Hours Maximum Marks : 80

General Instructions:

- (i) All questions are compulsory.
- (ii) The question paper consists of 34 questions divided into four sections A, B, C and D. Section A comprises of 10 questions of 1 mark each. Section B comprises of 8 questions of 2 marks each, Section C comprises of 10 questions of 3 marks each and Section D comprises of 6 questions of 4 marks each.
- (iii) Question numbers 1 to 10 in Section A are multiple choice questions where you are to select one correct option out of the given four.
- (iv) There is no overall choice. However, internal choice has been provided in 1 question of two marks, 3 questions of three marks each and 2 questions of four marks each. You have to attempt only one of the alternatives in all such questions.
- (v) Use of calculators is not permitted.

Section 'A'

Question numbers 1 to 10 are of one mark each.

1. The decimal expansion of the rational number $\frac{23}{2^35^2}$, will terminate after

how many places of decimal ?

(a) 1		(b) 3
(c) 4		(d) 5
Solution	Choice (h) is correct	

Solution. Choice (b) is correct. $\frac{23}{2^3 5^2} = \frac{23}{2(2^2)(5^2)} = \frac{23}{2(2 \times 5)^2} = \frac{23}{2(10)^2} = \frac{115}{100} = 0.115$

Thus, shows that decimal expansion of the rational number $\frac{23}{2^{3}5^{2}}$, will terminate after

three places of decimal.

2. If HCF (105, 120) = 15, then LCM (105, 120) is (a) 210(b) 420 (c) 840 (d) 1680 **Solution.** Choice (c) is correct. HCF × LCM = Product of two numbers $15 \times LCM = 105 \times 120$ LCM _Education Material Downloaded from http://www.evidyarthi.in/ GetLCBSE Notes, Video Tutorials, Test Papers & Sample Papers $LCM = 105 \times 8 = 840.$

3. In figure, the graph of a polynomial p(x) is shown. The number of zeroes of p(x) is



(a) 1 ·

(c) 3

Solution. Choice (b) is correct.

The number of zeroes of p(x) is 2 as the graph intersects the x-axis at two points A and B in figure.

4. The value of k for which 6x - 3y + 10 = 0 and 2x + ky + 9 = 0 has no solution is .
(a) -1
(b) -2
(c) 1
(d) 3

Solution. Choice (a) is correct.

Here $a_1 = 6$, $b_1 = -3$, $c_1 = 10$ and $a_2 = 2$, $b_2 = k$, $c_2 = 9$ The given system of equations will have no solution if

	<u>a</u> 1 _	$\underline{b_1}$	<u>c</u> 1
	a_2	b_2	c_2
⇒	$\frac{6}{2}$	$\frac{-3}{k}$	
⇒	k -	<u>-3×</u> 6	2

> k = -1

⇒

5. Let $\triangle ABC \sim \triangle PQR$, area of $\triangle ABC = 81 \text{ cm}^2$, area of $\triangle PQR = 144 \text{ cm}^2$ and QR = -6 cm, then length of *BC* is

 (a) 4 cm
 (b) 4.5 cm

 (c) 9 cm
 (d) 12 cm

Solution. Choice (b) is correct. Since $\triangle ABC \sim \triangle PQR$, therefore

 $\frac{\operatorname{area}\left(\Delta ABC\right)}{\operatorname{area}\left(\Delta PQR\right)} = \frac{BC^2}{QR^2}$ $\frac{81}{144} = \frac{BC^2}{QR^2}$ $\left(\frac{9}{12}\right)^2 = \left(\frac{BC}{QR}\right)^2$

 $\begin{bmatrix} \because \operatorname{area} (\Delta ABC) = \$1 \operatorname{cm}^2 (\operatorname{given}) \text{ and} \\ \operatorname{area} (\Delta PQR) = 144 \operatorname{cm}^2 (\operatorname{given}) \end{bmatrix}$

 $\frac{9}{12} = \frac{BC}{QR}$ $\frac{3}{4}$ $\frac{BC}{c}$ $[\forall QR = 6 \text{ cm} (\text{given})]$ $BC = \frac{9 \times 6}{4}$ \Rightarrow $BC = \frac{9 \times 3}{2}$ BC = 4.5 cm -6. The value of $\frac{\cos(90^\circ - \theta)\cos\theta}{\tan\theta} - 1$ is $(a) = \sin^2 \theta$ $(b) = \operatorname{cosec}^2 \Theta$ $(c) = \cos^2 \theta$ $(d) - \cot \theta$ Solution. Choice (a) is correct. $\frac{\cos\left(90^\circ-\theta\right)\cos\theta}{\tan\theta} - 1 = \frac{\sin\theta\cos\theta}{\tan\theta} - 1$ $= \frac{\sin\theta\cos\theta}{\sin\theta/\cos\theta} - 1$ = cos² 0 - 1 $= -(1 - \cos^2 \theta)$ $= -\sin^2 \theta$ 7. If $\tan \theta + \frac{1}{\tan \theta} = 2$, then the value of $\tan^2 \theta + \frac{1}{\tan^2 \theta}$ is (a) 3 (b) 4 (d) = 4(c) 2Solution. Choice (c) is correct. $\tan \theta + \frac{1}{\tan \theta} = 2$ Given. $\tan^2\theta + \frac{1}{\tan^2\theta} + 2\tan\theta - \frac{1}{\tan\theta} = 4$ $[:: (a+b)^2 = a^2 + b^2 + 2ab]$ $\tan^2 \theta + \frac{1}{\tan^2 \theta} + 2 = 4$ ------ $\tan^2 \theta \div \frac{1}{\tan^2 \theta} = 4 - 2$ _____ $\tan^2\theta + \frac{1}{\tan^2\theta} = 2$ _ 8. If 5 tan a = 4, then the value of $\frac{5\sin a - 3\cos a}{5\sin a + 2\cos a}$ is (a) $\frac{1}{3}$ (b) $\frac{2}{3}$ $(c)^{-}\frac{1}{6}$ (d) $\frac{2}{3}$ Educational Material Downloaded from http://www.evidyarthi.in/

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Solution. Choice (c) is correct.

5
$$\tan \alpha = 4 \Rightarrow \tan \alpha = \frac{4}{5}$$

 $5 \sin \alpha - 3 \cos \alpha$

 $5 \sin \alpha + 2 \cos \alpha$

 $(5 \sin \alpha - 3 \cos \alpha)/\cos \alpha$ $(5 \sin \alpha + 2 \cos \alpha)/\cos \alpha$ $5 \tan \alpha - 3 = 5(4/5) - 3$ $5 \tan \alpha + 2$ 5(4/5) + 2 $=\frac{4-3}{4+2}=\frac{1}{6}$

[Dividing numerator and denominator by $\cos \alpha$]

[∵ cosec (90° -- 8) = sec θ]

9. If sec 4A - cosec (A - 20°), where 4A is an acute angle, then the value of A is (b) 22°

 $(d) 24^{\circ}$

(a) 21°

(c) 23°

Solution. Choice (b) is correct.

Given $\sec 4A = \csc (A - 20^\circ)$

 $cosec (90^{\circ} - 4A) = cosec (A - 20^{\circ})$ =

 $90^{\circ} - 4A = A - 20^{\circ}$

 $4A + A = 90^{\circ} + 20^{\circ}$

 $5A = 110^{\circ}$

A - 22°

10. Which measure of central tendency is given by the x-coordinate of the point of intersection of 'more than ogive' and 'less than ogive' ?

(a) Mean

(b) Mode

(c) Median

(d) Mean and Median both.

Solution. Choice (c) is correct.

The median of a grouped data of central tendency is given by the x-coordinate of the point of intersection of the 'more than ogive' and 'less than ogive'.

Section B'

Question numbers 11 to 18 carry 2 marks each.

11. Write 21975 as a product of its prime factors.

Solution. We have

 $21975 = 5 \times 4395$

 $= 5 \times 5 \times 879$ $= 5 \times 5 \times 3 \times 293$

 $\approx 3 \times 5^2 \times 293.$

12. If the polynomial $x^4 + 2x^3 + 8x^2 + 12x + 18$ is divided by another polynomial $x^2 + 5$, the remainder comes out to be nx + q. Find the values of p and q.

Solution. We divide the given polynomial by $x^2 + 5$.

$$\frac{x^{2} + 2x + 3}{x^{2} + 5)x^{4} + 2x^{3} + 8x^{2} + 12x + 18} = \begin{bmatrix} \text{First term of quotient is } \frac{x^{4}}{x^{2}} = x^{2} \end{bmatrix}$$

$$\frac{x^{4} + 5x^{2}}{2x^{3} + 3x^{2} + 12x + 18} = \begin{bmatrix} \text{First term of quotient is } \frac{2x^{3}}{x^{2}} = 2x \end{bmatrix}$$

$$\frac{2x^{3} + 10x}{3x^{2} + 2x + 18} = \begin{bmatrix} \text{Second term of quotient is } \frac{2x^{3}}{x^{2}} = 2x \end{bmatrix}$$

$$\frac{3x^{2} + 2x + 18}{2x + 3} = \begin{bmatrix} \text{Third term of quotient is } \frac{3x^{2}}{x^{2}} = 3 \end{bmatrix}$$

So,
$$x^4 + 2x^3 + 8x^2 + 12x + 18 = (x^2 + 5)(x^2 + 2x + 3) + (2x + 3)$$

Quotient Remainder

But the given remainder is px + q. Therefore,

2x + 3 = px + qComparing both sides, we get : p = 2 and q = 3. Hence p = 2 and q = 3.

13. Solve the following system of equations :

$$\frac{1}{2x} - \frac{1}{y} = -1$$

$$\frac{1}{x} + \frac{1}{2y} = 8, \text{ where } x \neq 0, y \neq 0$$

Solution. The given system of equations can be written as :

$$\frac{1}{x} - \frac{2}{y} = -2$$
 (...(1)
[Multiplying both sides of both the given equations by 2]

and $\frac{2}{x} + \frac{1}{y}$

 $\frac{2}{x} + \frac{1}{y} = 16$...,(2)

Now, multiplying (2) by 2 and adding in (1), we get

$$\left(\frac{1}{x} - \frac{2}{y}\right) + 2\left(\frac{2}{x} + \frac{1}{y}\right) = -2 + 32$$

$$\Rightarrow \qquad \frac{1}{x} + \frac{4}{x} = 30$$

$$\Rightarrow \qquad \frac{5}{x} = 30$$

$$\Rightarrow \qquad x = \frac{5}{30} = \frac{1}{6}$$
Substituting $x = \frac{1}{6}$ in (1), we get
$$\frac{6 - \frac{2}{y}}{= -2}$$
Educational Material

$$\Rightarrow \qquad \frac{2}{y} = 6 \div 2$$

$$\Rightarrow \qquad y = \frac{2}{8} = \frac{1}{4}$$

Thus, the solution of the given system of equations is $x = \frac{1}{6}$ and $y = \frac{1}{4}$.
14. If sec $\alpha = \frac{5}{4}$, evaluate $\frac{1 - \tan \alpha}{1 + \tan \alpha}$.

Solution. Let us draw a right $\triangle ABC$ (see figure).

We have :
$$\sec \alpha = \frac{\text{Hypotenuse}}{\text{Base}}$$

 $\Rightarrow \qquad \frac{5}{4} = \frac{AC}{BC}$

 $\therefore AC = 5k, BC = 4k$, where k is a positive number Using the Pythagoras theorem, we have

	$AB^2 = AC^2 - BC^2$
,	$AB^2 = (5k)^2 - (4k)^2$
,	$AB^2 = 25k^2 - 16k^2 = 9k^2$
•	AB = 3k

$$\tan \alpha = \frac{AB}{BC} = \frac{3k}{4k} = \frac{3}{4}$$

Now,

$$\frac{-\tan\alpha}{+\tan\alpha} = \frac{1-(3/4)}{1+(3/4)} = \frac{(4-3)/4}{(4+3)/4} = \frac{4-3}{4+3} = \frac{1}{7}$$

Alternative Method :

 $\frac{1}{1}$

Given, $\sec \alpha = \frac{5}{4}$ $\Rightarrow \qquad \sec^2 \alpha = \frac{25}{16}$ $\Rightarrow \qquad 1 + \tan^2 \alpha = \frac{25}{16} - 1$ $\Rightarrow \qquad \tan^2 \alpha = \frac{25}{16} - 1$ $\Rightarrow \qquad \tan^2 \alpha = \frac{25 - 16}{16}$ $\Rightarrow \qquad \tan^2 \alpha = \frac{9}{16} = \left(\frac{3}{4}\right)^2$ $\Rightarrow \qquad \tan^2 \alpha = \frac{3}{4}$



 $\begin{array}{c|c}
 & A \\
 & 5k \\
 & 3k \\
\hline C & 4k \\
 & B \\
\end{array}$

Now,

 $\frac{1-(3/4)}{1+(3/4)} = \frac{(4-3)/4}{(4+3)/4}$ $\frac{1-\tan\alpha}{1+\tan\alpha}$

$$\frac{4-3}{4+3} = \frac{1}{7}$$

Prove that :

$$(\sin \theta + \cos e \theta)^{2} + (\cos \theta + \sec \theta)^{2} = 7 + \tan^{2} \theta + \cot^{2} \theta,$$

Solution. We have
L.H.S. = $(\sin \theta + \csc \theta)^{2} + (\cos \theta + \sec \theta)^{2}$
= $(\sin^{2} \theta + \csc^{2} \theta + 2 \sin \theta \cdot \csc \theta) + (\cos^{2} \theta + \sec^{2} \theta + 2 \cos \theta \cdot \sec \theta)$
= $(\sin^{2} \theta + \cos^{2} \theta) + \csc^{2} \theta + \sec^{2} \theta + 2 \sin \theta \cdot \frac{1}{\sin \theta} + 2 \cos \theta \cdot \frac{1}{\cos \theta}$
= $1 + (1 + \cot^{2} \theta) + (1 + \tan^{2} \theta) + 2 + 2$ [$\because \sec^{2} \theta = 1 + \tan^{2} \theta$; $\csc^{2} \theta = 1 + \cot^{2} \theta$]
= $(1 + 1 + 1 + 2 + 2) + \tan^{2} \theta + \cot^{2} \theta$
= $7 + \tan^{2} \theta + \cot^{2} \theta$
= $R.H.S.$
15. Prove that in the figure if *ABCD* is a trapezium with *AB* || *DC* || *EF*, then

BF FC

ED



Solution. Given : A trapezium ABCD in which $AB \parallel DC \parallel EF$.

To prove : $\frac{AE}{ED} = \frac{BF}{FC}$. **Proof** : In $\triangle ADC$, we have $EP \parallel DC$ $\frac{AE}{ED} = \frac{AP}{PC}$ Also, in $\triangle ABC$, we have PF || AB $\frac{AP}{PC} = \frac{BF}{FC}$ -From (1) and (2), we have $\frac{AE}{ED} = \frac{BF}{FC}$

Hence, proved.

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[$:: EF \parallel DC \text{ (given)}$] ...(1) [using BPT]

 $[:: EF \parallel AB \text{ (given)}]$

...(2) [using BPT]

16. In $\triangle ABC$, $\angle A = 90^{\circ}$ and $AD \perp BC$. Prove that $AB^{2} + CD^{2} = BD^{2} + AC^{2}$. Solution. Let ABC be a triangle such that $\angle A = 90^{\circ}$ and $AD \perp BC$.

We have to prove that

 $AB^2 + CD^2 = BD^2 + AC^2$

In right $\triangle ABD$, we have

 $AB^2 = AD^2 + BD^2 \quad ...(1) \text{ [using Pythagoras Theorem]}$ In right $\Delta ACD,$ we have

 $AC^2 = AD^2 + CD^2$...(2) [using Pythagoras Theorem]

Now, $AB^2 - AC^2 - (AD^2 + BD^2) - (AD^2 + CD^2)$ [using (1) and (2)]

$$= BD^2 - CL$$

$$\Rightarrow \quad AB^2 + CD^2 = BD^2 + AC^2$$

17. The following distribution gives the scores of 230 students of a school :

Scores	No. of students
400 450	
450 - 500	35
500 - 550	40
550 - 600	32
600 650	24
650 - 700	27
700 — 7 5 0	18
750 - 800	34
Total	230

Write the above distribution as more than type cumulative frequency distribution.

Solution. The cumulative frequency table by more than type method :

Scores	No. of students	Score more than	Cumulative frequency
400 - 450	20	400	230
450 - 500	35	450	210
500 - 550	40	500	175
550 - 600	32	550	135
600 - 650	24	60 0	103
650 - 700	27	650	79
700 - 750	18	700	52
750-800	34	750	34

We calculate more than cumulative frequencies by adding successive classes from bottom to top.

18. For the following grouped frequency distribution find the mode :

Class	3-6	6 - 9	9 - 12	12 - 15	15 – 18	18 - 21	21 – 24
Frequency	2	5	10	23	21	12	3

Solution. Here the maximum frequency is 23 and the class corresponding to this frequency is 12 - 15.



So, the modal class is 12 - 15. Lower limit (l) of the modal class = 12. Class size (h) = 15 - 12 = 3Frequency (f_1) of the modal class = 23 Frequency (f_0) of the class preceeding the modal class = 10 Frequency (f_2) of the class following the modal class = 21 Using the formula :

Mode =
$$l + \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \times h$$

= $12 + \frac{23 - 10}{2 \times 23 - 10 - 21} \times 3$
= $12 + \frac{13}{46 - 31} \times 3$
= $12 + \frac{13}{15} \times 3$
= $12 + \frac{13}{5}$
= $12 + 2.6 = 14.6$

Section 'C'

Question numbers 19 to 28 carry 3 marks each.

19. Show that any positive odd integer is of the form 6q + 1 or 6q + 3 or 6q + 5, where q is a positive integer.

Solution. Let a be any positive integer, when a is divided by 6. Then, by Euclid's division lemna, we get

 $a = 6q + r, 0 \le r < 6$, where q and r are whole numbers.

So, r = 0, 1, 2, 3, 4, 5.

-

When r = 0 or 2 or 4, then a becomes an even integer, *i.e.*, a = 6q or 6q + 2 or 6q + 4.

When r = 1 or 3 or 5, then a becomes a positive odd integer, *i.e.*, a = 6q + 1 or 6q + 3 or 6q + 5.

Hence any positive odd integer is of the form 6q + 1 or 6q + 3 or 6q + 5, where q is a positive integer.

20. Prove that $\sqrt{2} + \sqrt{5}$ is irrational.

Solution. Let us assume, to the contrary, that $\sqrt{2} + \sqrt{5}$ is a rational number. That is we can find coprime p and q ($q \neq 0$) such that

$$\sqrt{2} + \sqrt{5} = \frac{p}{q}$$
$$\frac{p}{q} - \sqrt{2} = \sqrt{5}$$
$$\left(\frac{p}{q} - \sqrt{2}\right)^2 = (\sqrt{5})$$

[Squaring both sides]



Since, p and q are integers, $\frac{p^2 - 3q^2}{2pq}$ is rational, and so $\sqrt{2}$ is rational.

But this contradicts the fact that $\sqrt{2}$ is irrational. So, we conclude that $\sqrt{2} + \sqrt{5}$ is **irrational**.

Or

Prove that $\frac{5\sqrt{2}}{7}$ is irrational.

 \Rightarrow

-

Solution. Let us assume to the contrary, that $\frac{5\sqrt{2}}{7}$ is a rational number.



Since $\frac{p}{q}$ is a rational number, therefore, $\frac{7}{5} = \frac{p}{q}$ is also rational number.

 $\Rightarrow \sqrt{2}$ is a rational number.

But this contradicts the fact that $\sqrt{2}$ is irrational.

This contradiction has arises because of our incorrect assumption that $\frac{5\sqrt{2}}{7}$ is rational.

So, we conclude that $\frac{5\sqrt{2}}{7}$ is irrational.

21. A two digit number is four times the sum of its digits and twice the product of the digits. Find the number.

Solution. Let the unit place digit be x and ten's place digit be y. Then, Original number = 10y + x

It is given that a two digit number is four times the sum of its digits.

$$\therefore \qquad 10y + x = 4(y + x)$$

$$\Rightarrow 10y - 4y = 4x - x$$

 $6\gamma = 3x$...(1) $x = 2\gamma$ Further, it is also given that a two digit number is twice the product of the digits. 10y + x = 2(xy)[using (1)]10y + 2y = 2[(2y)y]⇒ $12y = 4y^2$ $[\because y \neq 0]$ 3 = ySubstituting y = 3 in (1), we get x = 2(3) = 6Hence, the original number is **36**. Or Solve for x and y: $\frac{x}{a} + \frac{y}{b} = 2$ $ax - by = a^2 - b^2$ Solution. The given system of equations can be written as $\frac{x}{a} + \frac{y}{b} = 2 \Rightarrow \frac{bx + ay}{ab} = 2 \Rightarrow bx + ay = 2ab$ $ax - by = a^2 - b^2$...(1)...(2) and Multiplying (1) by b and (2) by a, we have ...(3) $b^2x + aby = 2ab^2$ $a^2x - aby = a^3 - ab^2$...(4) and Adding (3) and (4), we get $b^{2}x + a^{2}x = 2ab^{2} + a^{3} - ab^{2}$ $(b^2 + a^2)x = ab^2 + a^3$ ⇒ $(b^2 + a^2)x = a(b^2 + a^2)$ ⇒ $x = \frac{a(b^2 + a^2)}{(b^2 + a^2)}$ x = a Substituting x = a in (2), we get $a^2 - b\gamma = a^2 - b^2$ $by = a^2 - a^2 + b^2$ ⇒ $bv = b^2$ v = b⇒ Hence, x = a, y = b is the solution of the given system of equations. 22. If a and β are the zeroes of the quadratic polynomial $f(x) = 2x^2 - 5x + 7$, find the quadratic polynomial whose zeroes are $2\alpha + 3\beta$ and $3\alpha + 2\beta$. **Solution.** Since α and β are zeroes of the polynomial $2x^2 - 5x + 7$, therefore $\alpha + \beta = -\left(\frac{-5}{2}\right) = \frac{5}{2}$ $\alpha\beta = \frac{7}{2}$ and

Let S and P denote respectively the sum and product of zeroes of the required polynomial, then

·	$S = (2\alpha + 3\beta) + (3\alpha + 2\beta)$	
⇒	$S = 5\alpha + 5\beta = 5(\alpha + \beta) = 5 \times \frac{5}{\alpha} = \frac{25}{\alpha}$	
and ⇒	$P = (2\alpha + 3\beta)(3\alpha + 2\beta)$ $P = 6\alpha^2 + 4\alpha\beta + 9\alpha\beta + 6\beta^2$. •
⇒	$P = 6\alpha^2 + 6\beta^2 + 13\alpha\beta$	
⇒	$P = 6(\alpha^2 + \beta^2 + 2\alpha\beta) + \alpha\beta$	
⇒	$P = 6(\alpha + \beta)^2 + \alpha\beta$	
ر ج:	$P = 6 \left(\frac{5}{2}\right)^2 + \frac{7}{2}$	•
⇒,	$P = \frac{75}{2} + \frac{7}{2} = \frac{82}{2} = 41$	
Hence, the p	required polynomial $p(x)$ is given by : $p(x) = k(x^2 - Sx + P)$	
or p	$p(x) = k \left[x^2 - \frac{25}{2}x + 41 \right]$	•
or p	$p(x) = k(2x^2 - 25x + 82)$, where k is any non-zero real numbers.	mber.
23. Prove	that: $\frac{1+\cos A}{\sin A} + \frac{\sin A}{1+\cos A} = 2 \operatorname{cosec} A$	
Solution.	We have	
L.H.S.	$=\frac{1+\cos A}{\sin A}+\frac{\sin A}{1+\cos A}$	۰ <u>-</u>
	$= \frac{(1 + \cos A)^2 + \sin^2 A}{\sin A (1 + \cos A)}$	¥
	$= \frac{1 + 2\cos A + \cos^2 A + \sin^2 A}{\sin A (1 + \cos A)}$:
	$= \frac{1+2\cos A+1}{2}$	[stice
•	$\sin A \left(1 + \cos A\right)$	*
	$2 \pm 2 \cos 4$, - '
	$=\frac{2+2\cos A}{\sin A\left(1+\cos A\right)}$	• •
`,	$= \frac{2(1 + \cos A)}{\sin A (1 + \cos A)}$	
	$=\frac{2}{\sin A}$	
** 1	$= 2 \operatorname{cosec} A$	
· •	= RHS	ni.in/
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 $[::\cos^2 A + \sin^2 A = 1]$

24. Prove that

 $\frac{\sin \theta}{\cot \theta + \csc \theta} = 2 + \frac{\sin \theta}{\cot \theta - \csc \theta}$ Solution. We have

R.H.S. = $2 + \frac{\sin \theta}{\cot \theta - \csc \theta}$ $= 2 + \frac{\sin \theta \left(\cot \theta + \csc \theta \right)}{\left(\cot \theta - \csc \theta \right) \left(\cot \theta + \csc \theta \right)}$ $= 2 + \frac{\sin \theta \left(\cot \theta + \csc \theta \right)}{\cot^2 \theta - \csc^2 \theta}$ $= 2 + \frac{\sin \theta \cot \theta + \sin \theta \csc \theta}{\cot^2 \theta - (1 + \cot^2 \theta)}$ $= 2 + \frac{\sin\theta\cot\theta + \sin\theta}{\cos\theta} \\ \cos\theta$ $=\frac{-2^{4}+\sin\theta\cot\theta+1}{-1}$ $=\frac{-1+\sin\theta\cot\theta}{-1}$ $=\frac{1-\sin\theta\cot\theta}{1}$ $=\frac{1-\sin\theta\cot\theta}{\csc^2\theta-\cot^2\theta}$ $\sin\theta \csc\theta - \sin\theta \cot\theta$ $(\csc \theta + \cot \theta)(\csc \theta - \cot \theta)$ $\sin\theta (\csc\theta - \cot\theta)$ $(\operatorname{cosec} \theta + \operatorname{cot} \theta)(\operatorname{cosec} \theta - \operatorname{cot} \theta)$ $\sin \theta$ $\csc \theta + \cot \theta$

= L.H.S.

25. If ABC is an equilateral triangle with $AD \perp BC$, then prove that $AD^2 = 3DC^2$. Solution. Let ABC be an equilateral triangle and $AD \perp BC$.

$\ln \Delta AI$	DB and ΔADC , we have		Λ	
	AB = AC	[given]		
	$\angle B = \angle C$	$[Each = 60^{\circ}]$		
and	$\angle ADB = \angle ADC$	[Each = 90°]	· / \	
<i>:</i> .	$\Delta ADB \cong \Delta ADC$			
⇒	BD = DC	(1)		
<i>.</i>	BC = BD + DC = DC +	DC = 2DC(2) [using (1)]		١
1. E				1

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[:: $\sin \theta \cdot \csc \theta = 1$]

D

 $\overline{\mathbf{B}}$

 $[\because \operatorname{cosec}^2 \theta = 1 + \cot^2 \theta]$

In right angled $\triangle ADC$, we have

 $AC^2 = AD^2 + DC^2$ $BC^2 = AD^2 + DC^2$ <u>ک</u> $(2DC)^2 = \overline{AD}^2 + \overline{DC}^2$ $AD^2 = 4DC^2 - DC^2$ <u>__</u>

 $AD^2 = 3DC^2$

26. In figure, *DEFG* is a square and $\angle BAC = 90^{\circ}$. Show that $DE^2 = BD \times EC$.

[:: AC = BC, sides of an equilateral Δ]

[using (2)]



Solution. In $\triangle AGF$ and $\triangle DBG$, we have	·
$\angle GAF = \angle BDG$	$[Each = 90^{\circ}]$
$\angle AGF = \angle DBG$	[Corresponding $\angle s$]
So, by AA-criterion of similarity of triangles	, we have
$\Delta AGF \sim \Delta DBG$	(1)
In $\triangle AGF$ and $\triangle EFC$, we have	
$\angle FAG = \angle CEF$	$[Each = 90^{\circ}]$
$\angle AFG = \angle ECF$	[Corresponding $\angle s$]
So, by AA-criterion of similarity of triangles	, we have
$\Delta AGF \sim \Delta EFC$	(2)
From (1) and (2), we obtain	
$\Delta DBG \sim \Delta EFC$	
BD DG	• *
$\Rightarrow \qquad \overline{FE} = \overline{EC}$	• •
קת תק	
$\Rightarrow \frac{DD}{DE} = \frac{DE}{EQ}$	$[:: DEFG \text{ is a square.} \therefore EF = DE, DG = DE]$
\Rightarrow $UE = DU \times EU$.	

27. Find the mean of the following distribution, using step-deviation method :

Classes	Number of students
· <u>4-8</u>	2
8-12	12
12 - 16	15
. 16 – 20	25
20 - 24	18
24 - 28	12
28 - 32	13
32 - 36	8

Classes	Number of students (f)	Class-mark x _i	$d_i = x_i - 18$	$u_i = \frac{x_i - 18}{4}$	f _i u _i
4-8	2	6	- 12	- 3	- 6
8 - 12	12	10	- 8	-2	- 24
12 - 16	15	14	-4	1	-15
16 – 20	^{·.} 25	18	0	0	0
20 - 24	18	22	4	1	18
24 - 28	12	26	8	2	24
28 - 32	13	30	12	3 `	39
32 - 36	3	34	16	4	12
Total	$n = \Sigma f_i = 100$		en men de la constante de la co		$\Sigma f_i u_i = 48$

Solution. Let the assumed mean be a = 18 and h = 4. Calculation of Mean

From the table, $n = \Sigma f_i = 100$ and $\Sigma f_i u_i = 48$ Using the formula :

Mean
$$(\overline{X}) = a + \frac{\Sigma f_i u_i}{\Sigma f_i} \times h$$

 $\Rightarrow \qquad \overline{X} = 18 + \frac{48}{100} \times 4$
 $\Rightarrow \qquad \overline{X} = 18 + \frac{192}{100}$
 $\Rightarrow \qquad \overline{X} = 18 + 1.92$
 $\Rightarrow \qquad \overline{X} = 19.92$
Hence, mean is **19.92**.

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The mean of the following distribution is 196.8. Find the value of p.

Classes	0 - 80	80 - 160	160 - 240	240 - 3	320 320 - 400
Frequency	22	35	44	P P	24
Solution.		Calculation of	f Mean		-
· · Classes	Fr	equency (f _i)	Class-mark	(x _i)	$f_i x_i$
0 - 80		22	40		880
80 - 160		35	120	1	4200
160 - 240		44	200		8800
240 - 320		р	280		280p
320 - 400		24	360		8640
Total	~ n =	$\Sigma f_i = 125 + p$	· ·		$\Sigma f_i x_i = 22520 + 280p$

From the table, $n = \Sigma f_i = 125 + p$, $\Sigma f_i x_i = 22520 + 280p$ Using the formula :

$$Mean = \frac{\Sigma f_i x_i}{\Sigma f_i}$$

	$196.8 (minor) = \frac{22520 + 280p}{22520 + 280p}$
- .	130.0 (given) = 125 + p
÷	196.8(125 + p) = 22520 + 280p
⇒ ·	24600 + 196.8p = 22520 + 280p
⇒ ,	280p - 196.8p = 24600 - 22520
⇒́	83.2p = 2080
⇒	$n = \frac{2080}{1000}$
	. 83.2
⇒	p = 25
**	

Hence, the value of p is 25. -

28. Find the median of the following distribution :

0 100 9	
100 - 200 5	
200 - 300 9	
300 - 400 12	
400 – 500 17	
500 - 600 20	. (
600 - 700 15	
700 - 800 9	
800 - 900 7	s., t
900 - 1000 4	¢

Solution.

Calculation of Median

Marks	Frequence (f)	ry Cum	ulative frequency (cf)
0 – 100	2	W	2
100 – 200	. 5		7
200 - 300	9		16
300 - 400	12		28
400 - 500	17		45 (cf)
500 - 600	20 (f)	65
600 - 700	15		80
700 - 800	9		89
800 - 900	· 7 ·		96
900 - 1000	4.		100
Total	$n = \Sigma f_i = 1$	100 ,	

Here,
$$n = 100$$
 and $\frac{n}{2} = \frac{100}{2} = 50$.

Now, 500 - 600 is the class whose cumulative frequency is 65 is greater than $\frac{n}{2} = 50$. From the table, f = 20, cf = 45, h = 100Using the formula in

Median =
$$l + \frac{\frac{n}{2} - cf}{f} \times h$$

= $500 + \frac{50 - 45}{20} \times 100$
= $500 + \frac{500}{20}$
= $500 + 25 = 525$
Section 'D'

Question numbers 29 to 34 carry 4 marks each.

29. If two zeroes of the polynomial $x^4 + 3x^3 - 20x^2 - 6x + 36$ are $\sqrt{2}$ and $-\sqrt{2}$, find the other zeroes of the polynomial.

Solution. Since two zeroes are $\sqrt{2}$ and $-\sqrt{2}$, therefore $(x - \sqrt{2})(x + \sqrt{2}) = x^2 - 2$ is a factor of the given polynomial.

Now, we divide the given polynomial by $x^2 - 2$.

$$\frac{x^{2} + 3x - 18}{x^{2} - 2)x^{4} + 3x^{3} - 20x^{2} - 6x + 36}$$

$$\frac{x^{4} - 2x^{2}}{x^{4} - 2x^{2}}$$

$$\frac{x^{4} - 2x^{2}}{x^{3} - 18x^{2} - 6x + 36}$$

$$\frac{3x^{3} - 18x^{2} - 6x + 36}{6x}$$

$$\frac{-18x^{2} + 36}{-18x^{2} + 36}$$

$$\frac{-18x^{2} + 36}{0}$$

$$\frac{-18x^{2} + 36}{x^{2}}$$

$$\frac{-18x^{2} + 36}{x^{2}}$$

$$\frac{-18x^{2} + 36}{x^{2}} = -18$$

So,
$$x^4 + 3x^3 - 20x^2 - 6x + 36 = (x^2 - 2)(x^2 + 3x - 18)$$

= $(x - \sqrt{2})(x + \sqrt{2})[x^2 + 6x - 3x - 18]$
= $(x - \sqrt{2})(x + \sqrt{2})[x(x + 6) - 3(x + 6)]$
= $(x - \sqrt{2})(x + \sqrt{2})(x + 6)(x - 3)$

So, the zeroes of $x^2 + 3x - 18 = (x + 6)(x - 3)$ are given by x = -6 and x = 3. Hence, the other zeroes of the given polynomial are -6 and 3.

30. Prove that in a right triangle, the square of the hypotenuse is equal to the sum of the squares of the other two sides.

Solution. Given : A right triangle ABC, right angled at B. To prove : $(Hypotenuse)^2 = (Base)^2 + (Perpendicular)^2$

i.e.,

 $AC^2 = AB^2 + BC^2$

Construction : Draw $BD \perp AC$ **Proof :** $\triangle ADB \sim \triangle ABC$.

[If a perpendicular is drawn from the vertex of the right angle of a triangle to the hypotenuse then triangles on both sides of the perpendicular are similar to the whole triangle and to each other.]

So,	$\frac{AD}{AB} = \frac{AB}{AC}$
⇒ Í	$ADAC = AB^2$
Also, ΔBL	$DC \sim \Delta ABC$
So,	$\frac{CD}{BC} = \frac{BC}{AC}$
⇒ ·	$CD.AC = BC^2$
Adding (1) and (2), we have
AD.AC.+	$CD.AC = AB^2 + BC^2$
$\Rightarrow (AD + i)$	$CD)AC = AB^2 + BC^2$
⇒	$ACAC = AB^2 + BC^2$
Hence,	$AC^2 = AB^2 + BC^2$



[Sides are proportional]

...(1) [Same reasoning as above]

[Sides are proportional]

...(2)

Or

Prove that the ratio of areas of two similar triangles is equal to the square of their corresponding sides.

Solution. Given : $\triangle ABC$ and $\triangle PQR$ such that $\triangle ABC \sim \triangle PQR$.

To prove : $\frac{\operatorname{ar}(\Delta ABC)}{\operatorname{ar}(\Delta PQR)} = \frac{AB^2}{PQ^2} = \frac{BC^2}{QR^2} = \frac{CA^2}{RP^2}$

Construction : Draw $AD \perp BC$ and $PS \perp QR$.



$\angle ADB = \angle PSQ$	[Each = 90°]
$3rd \ \angle BAD = 3rd \ \angle QPS$ Thus $AADB$ and $APSO$ are equiangular and hence, they are similar	
Consequently $\frac{AD}{AB} = \frac{AB}{AB}$	(2)
PS PQ	nding sides in semal
If As are similar, the ratio of their correspo	inding sides is same
But $\frac{AB}{PQ} = \frac{BC}{QR}$	$[\because \Delta ABC \sim \Delta PQR]$
$\Rightarrow \qquad \frac{AD}{PS} = \frac{BC}{QR}$	(3) [using (2)]
Now, from (1) and (3), we get	1
$\frac{\operatorname{ar}\left(\Delta ABC\right)}{\operatorname{ar}\left(\Delta PQR\right)}=\frac{BC}{QR}\times\frac{BC}{QR}$	- - -
$\Rightarrow \qquad \frac{\operatorname{ar}\left(\Delta ABC\right)}{\operatorname{ar}\left(\Delta PQR\right)} = \frac{BC^2}{QR^2}$	(4)
As $ABC \sim APQR$, therefore	
AB BC CA	
$\frac{1}{PQ} = \frac{1}{QR} = \frac{1}{RP}$	
Hence, $\frac{\mathbf{ar} (\Delta ABC)}{\mathbf{ar} (\Delta PQR)} = \frac{AB^2}{PQ^2} = \frac{BC^2}{QR^2} = \frac{CA^2}{RP^2}$	[From (4) and (5)]
31. If $x = \tan A + \sin A$ and $y = \tan A - \sin A$, show that	
$x^2 - y^2 = 4\sqrt{xy}$	
Solution. Given, $\tan A + \sin A = x$	·(1)
and $\tan A - \sin A = y$	(2)
Adding (1) and (2), we get $2 \tan 4 - \pi + \alpha$	• (3) (
Subtracting (2) from (1), we get	(0)
$2\sin A = x - y$	(4)
Multiplying (3) and (4), we get	
$(x + y)(x - y) = (2 \tan A)(2 \sin A)$	(P \
$\Rightarrow x^2 - y^2 = 4 \tan A \sin A$	(a)
Now, $4\sqrt{xy} = 4\sqrt{(\tan A + \sin A)(\tan A - \sin A)}$	[using (1) and (2)]
$=4\sqrt{\tan^2 A - \sin^2 A}$	· · ·
$= 4\sqrt{\frac{\sin^2 A}{\cos^2 A} - \sin^2 A}$	
$=4\sqrt{\sin^2 A\left(\frac{1}{\cos^2 A}-1\right)}$	

$$= 4\sqrt{\sin^2 A \left(\frac{1-\cos^2 A}{\cos^2 A}\right)}$$

$$= 4\sqrt{\frac{\sin^2 A \cdot \sin^2 A}{\cos^2 A}}$$

$$= 4\frac{\sin A \cdot \sin A}{\cos^2 A}$$

$$= 4\frac{\sin A \cdot \sin A}{\cos^2 A}$$

$$= 4\left(\frac{\sin A}{\cos A}\right) \cdot \sin A$$

$$= 4 \tan A \sin A$$

$$= 4 \tan A \sin A$$
From (5) and (6), we obtain
$$x^2 - y^2 = 4 \tan A \sin A = 4\sqrt{xy}$$

$$\Rightarrow \qquad x^2 - y^2 = 4 \tan A \sin A = 4\sqrt{xy}$$

$$\Rightarrow \qquad x^2 - y^2 = 4 \tan A \sin A = 4\sqrt{xy}$$

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$$\Rightarrow \qquad x^2 - y^2 = 4 \tan A \sin A = 4\sqrt{xy}$$

$$\Rightarrow \qquad x^2 - y^2 = 4 \tan^2 + 4\sqrt{x}$$

$$= \frac{2}{3} \operatorname{cosec}^2 58^\circ - \frac{2}{3} \cot 58^\circ \tan (90^\circ - 58^\circ)$$

$$= \frac{5}{3} \tan 13^\circ \tan 37^\circ \tan 45^\circ \tan 90^\circ - 37^\circ) \tan (90^\circ - 13^\circ)$$

$$= \frac{2}{3} (\cos 2^\circ 58^\circ - \frac{2}{3} \cot^2 58^\circ - \frac{5}{3} (1) \tan 45^\circ (13^\circ 13^\circ 2 \tan 37^\circ 2 \cot 37^\circ)$$

$$= \frac{2}{3} (1 + \cot^2 58^\circ) - \frac{2}{3} \cot^2 58^\circ - \frac{5}{3} (1) \tan 45^\circ (1) \quad [\because \csc^2 \theta = 1 + \cot^2 \theta \text{ and } \tan \theta \cot \theta = 1]$$

$$= \frac{2}{3} - \frac{3}{3} = -1.$$

32. Prove that :
sin
$$\theta$$
 (1 + tan θ) + cos θ (1 + cot θ) = sec θ + cosec θ .
Solution. We have
L.H.S. = sin θ (1 + tan θ) + cos θ (1 + cot θ)
= (sin θ + sin θ tan θ) + (cos θ + cos θ cos θ)
= (sin θ + sin θ $\frac{\sin \theta}{\cos \theta}$ + $\left(\frac{\sin^2 \theta}{\cos \theta} + \frac{\cos^2 \theta}{\sin \theta}\right)$
= (sin θ + cos θ) + $\left(\frac{\sin^2 \theta}{\sin \theta} + \frac{\cos^2 \theta}{\sin \theta}\right)$
= (sin θ + cos θ) + $\left(\frac{\sin^2 \theta + \cos^2 \theta}{\sin \theta \cos \theta}\right)$
= (sin θ + cos θ) + $\frac{(\sin \theta + \cos \theta)(\sin^2 \theta + \cos^2 \theta - \sin \theta \cos \theta)}{\sin \theta \cos \theta}$
[:: $a^3 + b^3 = (a + b)(a^2 + b^2 - ab)]$
= (sin θ + cos θ) $\left[1 + \frac{\sin^2 \theta + \cos^2 \theta - \sin \theta \cos \theta}{\sin \theta \cos \theta}\right]$
= (sin θ + cos θ) $\left[1 + \frac{\sin^2 \theta + \cos^2 \theta - \sin \theta \cos \theta}{\sin \theta \cos \theta}\right]$
= (sin θ + cos θ) $\left[1 + \frac{\sin^2 \theta + \cos^2 \theta - \sin \theta \cos \theta}{\sin \theta \cos \theta}\right]$
= (sin θ + cos θ) $\left[1 + \frac{\sin^2 \theta + \cos^2 \theta - \sin \theta \cos \theta}{\sin \theta \cos \theta}\right]$
= (sin θ + cos θ) $\left[1 + \frac{\sin^2 \theta + \cos^2 \theta - \sin \theta \cos \theta}{\sin \theta \cos \theta}\right]$
= (sin θ + cos θ) $\left[1 + \frac{\sin^2 \theta + \cos^2 \theta - \sin \theta \cos \theta}{\sin \theta \cos \theta}\right]$
= (sin θ + cos θ) $\left[1 + \frac{\cos^2 \theta + \sin^2 \theta \cos^2 \theta}{\sin \theta \cos \theta}\right]$
= (sin θ + cos θ) $\left[\frac{\sin \theta \cos \theta + 1 - \sin \theta \cos \theta}{\sin \theta \cos \theta}\right]$
= $\frac{\sin \theta}{\sin \theta \cos \theta} + \frac{\cos \theta}{\sin \theta \cos \theta}$
= $\frac{\sin \theta}{\sin \theta \cos \theta} + \frac{\cos \theta}{\sin \theta \cos \theta}$
= $\frac{1}{\cos \theta} + \frac{\sin \theta}{\sin \theta \cos \theta}$

33. The coach of a cricket team buys 3 bats and 6 balls for $\overline{1300}$. Later, he buys another bat and 3 more balls of the same kind for $\overline{1300}$. Represent this situation algebraically and geometrically.

Solution. Let the price of a bat be $\forall x$ and that of a ball be $\forall y$.

It is given that the coach buys 3 bats and 6 balls for ₹ 3900.

 $\therefore \qquad 3x + 6y = 3900$

Also, it is given that the coach buys another bat and 3 more balls for ₹ 1300.

 $\therefore \qquad x + 3y = 1300$

The algebraic representation of the given conditions is

3x + 6y = 3900x + 3y = 1300

Geometrical representation : Let us draw the graphs of the equations (1) and (2). For this, we find two solutions of each of the equations which are given in tables.

3x + 6y = 3900			
x	0	1300	
γ	650	0	

x + 3y = 1300			
x	100	1300	
У	400	0	

1 1 1 1

Plot the points A(0, 650), B(1300, 0), C(100, 400) and B(1300, 0) on graph paper and join the points to form the lines AB and BC as shown in figure.

The two lines (1) and (2) intersect at the point B(1300, 0). So, x = 1300, y = 0 is the required solution of the pair of linear equations.



34. The lengths of 40 leaves of a plant are measured correct to the nearest millimetre, and the data obtained is represented in the following table :

Length (in mm)	Number of leaves
118 - 126	3
127 - 135	5
136 - 144	9
145 - 153	. 12
154 - 162	5
163 - 171	4
172 - 180	2

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Draw a more than type ogive for the given data. Hence, obtain the median length of the leaves from the graph and verify the result by using the formula.

Length	Number of leaves	Length more	Cumulative
(in mm)	[Frequency (f)]	than	frequency (cf)
117.5 - 126.5	3 .	117.5	40
126.5 - 135.5	5	126.5	37
135.5 - 144.5	9	135.5	32
144.5 - 153.5	12	144.5	23
153.5 - 162.5	. 5	153.5	11
162.5 - 171.5	4	162.5	6
171.5 - 180.5	2	171.5	2

Solution. The given frequency distribution is not continuous. So, we first make it continuous and prepare the cumulative frequency table by more than type given below :

Other than the given class-interval, we assume that the class-interval 180.5 - 189.5 with zero frequency. Now, we mark the lower class limits on x-axis and the cumulative frequencies along y-axis on suitable scales to plot the points (117.5, 40), (126.5, 37), (135.5, 32), (144.5, 23), (153.5, 11), (162.5, 6), (171.5, 2). We join these points with a smooth curve to get the "more than" ogive as shown in the figure.



From this point, draw a line parallel to the x-axis cutting the curve at a point. From this point, draw a perpendicular to the x-axis. The point of intersection of this perpendicular with the x-axis determine the median length of the data (see figure), i.e., median length is 146.75 mm.

To calculate the median length, we need the frequency distribution table with the given cumulative frequency.

Table			
Class interval	Frequency (f)	Cumulative frequency (cf)	
117.5 - 126.5	3	3	
126.5 - 135.5	5	8	
135.5 - 144.5	<u>9</u> .	17	
144.5 - 153.5	12	29	
153.5 - 162.5	5	34	
162.5 - 171.5	4	38	
171.5 - 180.5	2	40	

Now, 144.5 - 153.5 is the class whose cumulative frequency is 29 is greater than $\frac{n}{2} = \frac{40}{2} = 20$

 \therefore 144.5 – 153.5 is the median class. From the table : f = 12, cf = 17, h = 9Using the formula :

Median =
$$l + \frac{\left(\frac{n}{2} - cf\right)}{f} \times h$$

= 144.5 + $\frac{(20 - 17)}{12} \times 9$
= 144.5 + $\frac{27}{12}$
= 144.50 + 2.25
= 146.75 mm

So, about half the leaves have length less than 146.75 mm and the other half have length more than 146.75 mm.