

Sample Paper-02 (unsolved)
Mathematics
Class - XI

Time allowed: 3 hours

Maximum Marks: 100

General Instructions:

- a) All questions are compulsory.
- b) The question paper consists of 26 questions divided into three sections A, B and C. Section A comprises of 6 questions of one mark each, Section B comprises of 13 questions of four marks each and Section C comprises of 7 questions of six marks each.
- c) All questions in Section A are to be answered in one word, one sentence or as per the exact requirement of the question.
- d) Use of calculators is not permitted.

Section A

1. Write a trigonometric function that is even, its domain and range.
2. Prove that $f(x) - f(-x)$ is an odd function.
3. Write the equation of tangent to the circle $x^2 + y^2 = 13$ at the point (3, 2)
4. Evaluate i^{62}
5. Write the condition that the ellipse represented by the equation $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ whose major axis coincides with the line $x = 0$
6. In how many ways can 5 students be seated at a (1) round table (2) on a bench

Section B

7. $f(x-1) = 3x^4 - 12x^3 + 13x^2 - 2x + 7$ Find $f(x)$
8. Find the largest term in the expansion of $(3 - 2x)^9$ when $x = 1$
9. Find the condition that the equations $ax^2 + bx + c = 0$, $px^2 + qx + r = 0$ have a common root
10. Prove by mathematical induction that for all positive integral values of n , $(10^n - 1)$ is divisible by 9
11. Find the domain and range of the function $f(x) = \frac{1}{3 - \sin 3x}$
12. Find the limit $\lim_{x \rightarrow 0} \frac{\sin x}{x}$
13. Solve $\tan \theta + \tan 2\theta - 3 \tan \theta \tan 2\theta = 3$
14. If $f(x-1) = x^2 - 2x$ Find $f^{-1}(17)$

15. Prove that if a, b are the intercepts made by a line with x axis and y axis respectively such that $\frac{1}{a} + \frac{1}{b} = k$ where k is a constant then the line passes through a fixed point. Also find the fixed points
16. Find the least positive value of n if $\frac{1+i}{1-i}^n = -1$
17. Find the range of $f(x)$ when $f(x) = a \cos x + b \sin x$
18. Find the non-zero solutions of $1 + 2i \cdot i^x = 5$
19. In single throw of two dies find the probability of getting a minimum sum of 9

Section C

20. Prove that A, G, H form a decreasing GP where A, G, H are the AM, GM, HM between two numbers (a, b)
21. A bag contains tickets numbered from 1 to 10. Two tickets are drawn at random. Find the probability that both are prime.
22. One reporter tells lie in 30% cases and the other in 35% cases. Find the probability that both contradict each other on the same report.
23. Differentiate $\cos x$ from the first principle with respect to x
24. Find the sum of n terms of the series $1^3 + 2^3 + 3^3 + \dots + n^3$
25. Find the foci and the equation to the directrix of the ellipse represented by the equation $\frac{x^2}{16} + \frac{y^2}{25} = 1$
26. Calculate the mean deviation from the median for the following data
- | | | | | | | | | | |
|--------------|----|----|----|----|----|----|----|----|----|
| Weight in Kg | 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 |
| No of men | 10 | 8 | 15 | 20 | 35 | 35 | 22 | 20 | 15 |