MODEL TEST PAPER 10 FIRST TERM (SA-I) MATHEMATICS

(With Answers)

CLASS X

Time Allowed : 3 to 3½ Hours] [Maximum Marks : 80

General Instructions :

- (i) All questions are compulsory.
- (ii) The question paper consists of 34 questions divided into four sections A, B, C and D. Section A comprises of 10 questions of 1 mark each, Section B comprises of 8 questions of 2 marks each, Section C comprises of 10 questions of 3 marks each and Section D comprises of 6 questions of 4 marks each.
- (iii) Question numbers 1 to 10 in Section A are multiple choice questions where you are to select one correct option out of the given four.
- (iv) There is no overall choice. However, internal choice has been provided in 1 question of two marks, 3 questions of three marks each and 2 questions of four marks each. You have to attempt only one of the alternatives in all such questions.
- (v) Use of calculators is not permitted.

Section 'A'

Question numbers 1 to 10 are of one mark each.

1. If $\cot \theta = \frac{5}{2}$, then the value of $\frac{(2+2 \csc \theta)(1-\csc \theta)}{(2+2 \sec \theta)(1-\sec \theta)}$ is (a) $\frac{625}{16}$ (b) $\frac{615}{16}$ (c) $\frac{635}{16}$ (d) $\frac{605}{16}$

2. If the pair of linear equations 10x + 5y - (k - 5) = 0 and 20x + 10y - k = 0 has infinitely many solutions, then the value of k is

(a) $\{$	5	(b)	10
(c)	2	(d)	8

3. Which of the following numbers has non-terminating repeating decimal expansion?

(a)	17	(h)	<u>7</u>
(4)	320	(0)	80
(n)	84	(d)	- 93
(0)	400	(a)	420
4.	$(\operatorname{cosec} \theta - \sin \theta)(\operatorname{sec} \theta - \cos \theta)(\tan \theta + \cot \theta)$)) is	equal to
(a)	0	<i>(b)</i>	1 ·
(c)	-1	(d)	none of these
5.	If $\sec 2\theta = \csc (\theta - 45^\circ)$ where 2θ is an a	acute	e angle, then θ is equal
(a)	42°	(b)	43°
(c)	44°	(d)	45°
	(29	1)	
			·

Educational Material Downloaded from http://www.evidyarthi.in/ Get CBSE Notes, Video Tutorials, Test Papers & Sample Papers

to

6. If $x \cos (90^\circ - \theta) \tan (90^\circ - \theta) = \sin (90^\circ - \theta)$, then x is equal to

(a) $\frac{1}{2}$ (b) $\frac{1}{\sqrt{2}}$

(c) 1

7. In figure, $DE \parallel CA$ and D is a point on BC such that BD : DC = 2 : 3. The ratio of erea of $\triangle ABC$ to area of $\triangle BDE$ is

(d) $\sqrt{3}$



(a) 25;4 (c) 25:18

8. In figure, the graph of a polynomial p(x) is shown. The number of zeroes of p(x) is



'(a) 0

(c) 2

9. For a given data with 70 observations the less than ogive' and the 'more than ogive' intersect at (20.5, 35). The median of the data is

(a)	20	(b)	35
· (c)	70 .	(d)	20.5
10.	If HCF (84, 630) = 42 then LCM (84, 630)) is	
(a)	1240	(b)	1260
(c)	-1280	(d)	1200

Section 'B'

Question numbers 11 to 18 carry 2 marks each.

11. Determine the values of a and b for which the following pair of linear equations has infinite many solutions :

 $\Im \mathbf{x} - (a + 1)\mathbf{y} = 2b - 1$

5x + (1-2a)y = 3b

12. Show that every positive even integer is of the form 2q and every odd positive integer is of the form 2q + 1 where q is some whole number.

13. On dividing the polynomial $3x^3 - 4x^2 - 3x + 25$ by a polynomial g(x), the quotient and remainder were 3x + 5 and 5 respectively, find g(x).

14. Prove that :

$$\frac{\tan^2 A}{1 + \tan^2 A} + \frac{\cot^2 A}{1 + \cot^2 A} = 1$$

Prove that :

 $\frac{\cot A - 1}{2 - \sec^2 A} = \frac{\cot A}{1 + \tan A}$

15. In figure, AB || DE and BD || EF. Prove that $CD^2 = AC \times FC$.



16. In $\triangle ABC$, $AD \perp BC$ and $AD^2 = BD \times CD$. Prove that $\angle BAC$ is a right angle.



17. A life insurance agent found the following data for distribution of ages of 100 policy holders, when the policies are given only to persons having age 18 years but less than 60 years.

Age (in years)	0 2 0	20-25	25 – 30	30 – 3 5	35-40	40 - 45	45 - 50	50 - 55	55 - 60
No. of policy holders	2	4	18	21	33	11	3	6	2

Write the above distribution as less than type cumulative frequency distribution.

18. Find the mode of the following distribution of house-hold expenditure (in \mathfrak{T}) of manual workers in a city :

Expenditure (in ₹)	Frequency	Expenditure (in ₹)	Frequency
1000 2 000	24	(5000 - 6000	30
2000 - 3000	4 0	6000 - 7000	22
3000 - 4000	33	7000 - 8000	16
4000 - 5000	28	8000 - 9000	7

Section 'C'

Question numbers 19 to 28 carry 3 marks each.

19. Show that 21^n cannot end with the digits 0, 2, 4, 6 and 8 for any natural number n.

20. Prove that $\frac{13}{7}\sqrt{5}$ is irrational.

Оr

Prove that $\sqrt{3} + \sqrt{5}$ is irrational.

21. Student of a class are made to stand in (complete) rows. If 4 students are extra in a row there would be two rows less. If four students are less in a row there would be four more rows. Find the number of students in the class.

Or

A and B have some money with them. A said to B, 'If you give me \gtrless 100, my money, will become 75% of the money left with you'. B said to A, 'Instead if you give me \gtrless 100, your money will become 40% of my money'. How much money did A and B have originally ?

22. If α , β are zeroes of the polynomial $x^2 - 2x - 15$, then form a quadratic polynomial whose zeroes are (2α) and (2β) .

23. Prove that :

$$\frac{\sin\theta}{1+\cos\theta} + \frac{1+\cos\theta}{\sin\theta} = 2\csc\theta$$

24. Prove that :

$$\frac{\sin^2 A}{\cos^2 A} + \frac{\cos^2 A}{\sin^2 A} = \frac{1}{\sin^2 A \cos^2 A} - 2$$

25. A ladder reaches a window which is 12 m above the ground on one side of the street. Keeping its foot at the same point is turned to the other side of the street to reach a window 9 m high. Find the width of the street if the length of the ladder is 15 m.

26. In figure, $\triangle ABC$ and $\triangle AMP$ are right angled at B and M respectively, prove that $CA \times MP = PA \times BC$



27. Find the median of the following data :

Age (in years)	20 - 25	25 - 30	30 - 35	35 - 40	40 - 45	45 - 50	50 55	55 - 60
No. of Persons	50	70	100	180	150	120	70	59

28. Find the mean of the following distribution using step-deviation method.

Income (in ₹)	0 - 50	50 - 100	100 - 150	150 - 200	200 - 250	250 - 300
Frequency	90	150	100	80	70	10 ·

0r

The mean of 10 numbers is 12.5. The mean of first six numbers is 15 and the mean of last five numbers is 10. Find the sixth number.

Section D'

Question numbers 29 to 34 carry 4 marks each. 29. Prove that :

$$\frac{\tan\theta}{1-\tan\theta} - \frac{\cot\theta}{1-\cot\theta} = \frac{\cos\theta + \sin\theta}{\cos\theta - \sin\theta}$$

Evaluate :

$\sin (90^\circ - \theta) \cdot \csc (90^\circ - \theta) \cot \theta$	$\sin^2 \frac{65^\circ + \sin^2 25^\circ}{25^\circ}$
$\sec (90^\circ - \theta) \cdot \cos (90^\circ - \theta) \tan (90^\circ - \theta)$	tan 1.0° tan 35° tan 55° tan 80

+ 2 $\cos^2 32^\circ \csc^2 58^\circ - \cos^2 45^\circ$ 30. Find all the zeroes of the polynomial $f(x) = 2x^4 - 3x^3 - 3x^2 + 6x - 2$, if two of its zeroes are

 $\sqrt{2}$ and $-\sqrt{2}$.

31. Prove that ;

$$\sin^{8}\theta - \cos^{8}\theta = (\sin^{2}\theta - \cos^{2}\theta)(1 - 2\sin^{2}\theta\cos^{2}\theta)$$

32. Solve the following system of linear equations graphically :

2.

$$2x + y = 8$$
$$3x - 2y = 12$$

Also find the coordinates of the points where these lines meet the x-axis.

33. The annual profits earned by 30 shops of a shopping complex in a locality give rise to the following distribution :

Profit (in lakhs ₹)	Number of shops (frequency)
More than or equal to 5	30
More than or equal to 10	28
More than or equal to 15	· 16 -
More than or equal to 20	14
More than or equal to 25	10
More than or equal to 30	7
More than or equal to 35	3

Draw both ogives for the data above.

34. Prove that the ratio of the areas of two similar triangles is equal to the ratio of the squares of their corresponding sides.

 $\mathbf{0}r$

Prove that in a right triangle, the square of the hypotenuse is equal to the sum of the squares of the other two sides.

ANSWERS Section 'A'

Educational Material Downloaded from http://www.evidyarthi.in/ Get CBSE Notes, Video Tutorials, Test Papers & Sample Papers

3. (d)

 $\mathbf{1}_{\bullet}$ (a)

4.	(b)	*	5.	(d)		6.	(c)
7.	(c)		8.	(b)	•	9.	(d)
10	(b)						

Section B'

11. a = 8, b = 5

13. $g(x) = x^2 - 3x + 4$

17.

Age (in years)	No. of policy holders (cf)
Less than 20	2
Less than 25	6
Less than 30	24
Less than 35	45
Less than 40	78
Less than 45	89
Less than 50	92
Less than 55	98
Less than 60	100

18. Mode = 2695.65

Section 'C'

19. Hint:
$$21^n = (7 \times 3)^n = 7^n \times 3^n$$

If 21^n ends with any one of the digits 0, 2, 4, 6 or 8, then it must be divisible by $2 \Rightarrow 2$ divides 21^n but 2 is prime $\Rightarrow 2$ divides 21, which is wrong.

So, 21^n cannot end with the digits 0, 2, 4, 6 or 8 for any natural number n.

21. Number of students in the class = 96 Or Originally A have money = ₹ 500, Originally B have money = ₹ 900

22. $x^2 - 4x - 60$

- 25. Width of the street = 21 m
- **27.** Median = 39.9 years
- **28.** Mean = 117 Or Sixth number is 15.

Section 'D'

29. $O_{T} = \frac{7}{2}$

30. The zeroes of the polynomial f(x) are $\sqrt{2}$, $-\sqrt{2}$, 1 and $\frac{1}{2}$.

32. x = 4, y = 0; (0, 8) and (0, -6)