

Solutions to JEE(MAIN)-2013 XYZ

PAPER - 1 : CHEMISTRY, MATHEMATICS & PHYSICS

Test Booklet Code

Read carefully the Instructions on the Back Cover of this Test Booklet.



Important Instructions:

- 1. Immediately fill in the particulars on this page of the Test Booklet with *Blue/Black Ball Point Pen. Use of pencil is strictly prohibited.*
- 2. The test is of **3 hours duration**.
- 3. The Test Booklet consists of 90 questions. The maximum marks are 360.
- 4. There are *three* parts in the question paper A, B. C consisting of **Chemistry**, **Mathematics** and **Physics** having 30 questions in each part of equal weightage. Each question is allotted 4 (four) marks for correct response.
- 5. Candidates will be awarded marks as stated above in instruction No. 4 for correct response of each question. (1/4) (one fourth) marks will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer sheet.
- 6. There is only one correct response for each question. Filling up more than one response in any question will be treated as wrong response and marks for wrong response will be deducted accordingly as per instruction 5 above.

PART A	-CHEMISTRY	

	PARTA -CI	HEMISTRY
1.	secondary or tertiary. Which alcohol reacts fastest	
	(1) tertiary alcohol by $S_N 1$ (3) tertiary alcohol by $S_N 2$	(2) secondary alcohol by $S_N 2$ (4) secondary alcohol by $S_N 1$
Sol.	(1) Reaction proceeds through carbocation formation through S_N1 with 3^0 alcohol.	as 3 ⁰ carbocation is highly stable, hence reaction proceeds
2	The first ionization potential of Na is 5.1 eV. The	value of electron gain enthalpy of Na ⁺ will be:
	$(1) - 5.1 \mathrm{eV}$	(3) -10.2 eV
	(3) $+ 2.55 \text{ eV}$	(4) $-2.55 \mathrm{eV}$
ol.	(1)	
	$Na \xleftarrow{\Delta H = +5.1eV}{Na^+ + e^-}$, here the backward r	eaction releases same amount of energy and known as
	Electron gain enthalpy.	
	Stability of the species Li_2 , Li_2^- and Li_2^+ increases	s in the order of:
	(1) $\text{Li}_2^- < \text{Li}_2^+ < \text{Li}_2$	(3) $\text{Li}_2 < \text{Li}_2^- < \text{Li}_2^+$
	(3) $\text{Li}_2^- < \text{Li}_2 < \text{Li}_2^+$	(4) $\text{Li}_2 < \text{Li}_2^+ < \text{Li}_2^-$
ol.	(1)	
	$Li_2(6) = \sigma ls^2 \sigma^2 ls^2 \sigma 2s^2$	
	B.O. = $\frac{4-2}{2} = 1$	
	$\mathrm{Li}_{2}^{+}(5) = \sigma \mathrm{ls}^{2} \overset{\sigma}{\sigma} \mathrm{ls}^{2} \sigma 2 \mathrm{s}^{1}$	
	B. O. $=\frac{3-2}{2}=0.5$	
	$\mathrm{Li}_{2}^{-}(7) = \sigma \mathrm{ls}^{2} \overset{*}{\sigma} \mathrm{ls}^{2} \sigma \mathrm{2s}^{2} \overset{*}{\sigma} \mathrm{2s}^{1}$	
	B.O. $=\frac{4-3}{2}=0.5$	
	Li_2^+ is more stable than Li_2^- because Li_2^- has more	re numbers of antibonding electrons.
		mL of 0.5 (M) HCl with 250 mL of 2(M)HCl will be:
	(1) 1.00 M (3) 0.975 M	(2) 1.75 M (4) 0.875 M
iol.	(4)	
	$\mathbf{M}_1 \mathbf{V}_1 + \mathbf{M}_2 \mathbf{V}_2 = \mathbf{M} \mathbf{V}$	
	$M = \frac{M_1 V_1 + M_2 V_2}{V} = \frac{0.5 \times 750 + 2 \times 250}{1000}$	
	M = 0. 875	
	Which of the following is the wrong statement?	
	(1) O_3 molecule is bent	(2) Ozone is violet-black in solid state
	(3) Ozone is diamagnetic gas	(4) ONCl and ONO ⁻ are not isoelectronic
ol.	(All the options are correct statements)	
	(1) Correct, as O	

- (2) Correct, as ozone is violet-black solid.
- (3) Correct, as ozone is diamagnetic.
- (4) Correct, as ONCI = 32 electrons and $ONO^{-} = 24$ electron hence are not isoelectronic.
- All options are correct statements.
- 6. Four successive members of the first row transition elements are listed below with atomic numbers. Which one of them is expected to have the highest $E^0_{\mathsf{M}^{3*}/\mathsf{M}^{3*}}$ value?
 - (1) Mn(Z = 25)(2) Fe(Z = 26)(3) Co(Z = 27)(4) Cr(Z = 24)
- Sol.

(3)

 $E^{0}_{Mn^{+3}/Mn^{+2}} = 1.57 V$ $E_{Fe^{+3}/Fe^{+2}}^{0} = 0.77 V$ $E_{Co^{+3}/Co^{+2}}^{0} = 1.97 V$ $E^0_{Cr^{+3}/Cr^{+2}} = -0.41 V$

- 7. A solution of (-) -1 - chloro -1 - phenylethane is toluene racemises slowly in the presence of a small amount of SbCl₅, due to the formation of :
 - (1) carbene (2) carbocation (4) carbanion
 - (3) free radical

Sol. (2)

The coagulating power of electrolytes having ions Na⁺, Al³⁺ and Ba²⁺ for arsenic sulphide sol increases in 8. the order:

(1)	$Na^{+} < Ba^{2+} < Al^{3+}$	(2) $Ba^{2+} < Na^+ < Al$	5+
(3)	$Al^{3+} < Na^+ < Ba^{2+}$	(4) $Al^{3+} < Ba^{2+} < Na$	1 ⁺

Sol.

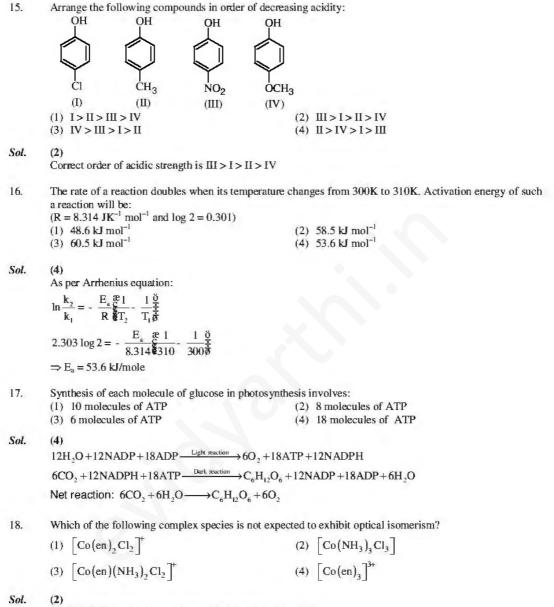
(1)

As₂S₃ is an anionic sol (negative sol) hence coagulation will depend upon coagulating power of cation, which is directly proportional to the valency of cation (Hardy-Schulze rule).

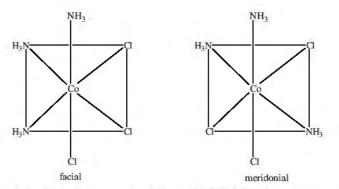
- 9. How many litres of water must be added to 1 litre of an aqueous solution of HCl with a pH of 1 to create an aqueous solution with pH of 2? (1) 0.9 L (2) 2.0 L (3) 9.0 L (4) 0.1 L
- Sol. (3) Initial pH = 1, i.e. $[H^+] = 0.1$ mole/litre New pH = 2, i.e. $[H^+] = 0.01$ mole/litre In case of dilution: $M_1V_1 = M_2V_2$ $0.1 \times 1 = 0.01 \times V_2$ $V_2 = 10$ litre. Volume of water added = 9 litre.
- 10. Which one of the following molecules is expected to exhibit diamagnetic behaviour? (2) O₂ (1) N₂ (3) S₂ (4) C₂
- Sol. (1) & (4) both are correct answers.
 - $N_2 \rightarrow Diamagnetic$
 - $O_2 \rightarrow Paramagnetic$
 - $S_2 \rightarrow Paramagnetic$

 $C_2 \rightarrow Diamagnetic$

	$C_2 \rightarrow Diamagnetic$
11.	Which of the following arrangements does not represent the correct order of the property stated against it ? (1) $Ni^{2+} < Co^{2+} < Fe^{2+} < Mn^{2+}$: ionic size (2) $Co^{3+} < Fe^{3+} < Cr^{3+} < Sc^{3+}$: stability in aqueous solution (3) $Sc < Ti < Cr < Mn$: number of oxidation states (4) $V^{2+} < Cr^{2+} < Mn^{2+} < Fe^{2+}$: paramagnetic behaviour
Sol.	(2) & (4) both are correct answers) The exothermic hydration enthalpies of the given trivalent cations are: $Sc^{+3} = 3960 \text{ kJ/mole}$ $Fe^{+3} = 4429 \text{ kJ/mole}$ $Co^{+3} = 4553 \text{ kJ/mole}$ $Cr^{+3} = 4553 \text{ kJ/mole}$ Hence Sc^{+3} is least hydrated; so least stable (not most stable) Fe^{+2} contains 4 unpaired electrons where as Mn ⁺² contains 5 unpaired electrons hence (4) is incorrect.
12.	Experimentally it was found that a metal oxide has formula $M_{0.98}O$. Metal M, is present as M^{2+} and M^{3+} in its oxide. Fraction of the metal which exists as M^{3+} would be: (1) 4.08% (2) 6.05% (3) 5.08% (4) 7.01%
Sol.	(1) Metal oxide = $M_{0.98}O$ If 'x' ions of M are in +3 state, then $3x + (0.98 - x) \times 2 = 2$ x = 0.04 So the percentage of metal in +3 state would be $\frac{0.04}{0.98} \times 100 = 4.08\%$
13.	A compound with molecular mass 180 is acylated with CH ₃ COCl to get a compound with molecular mass 390. The number of amino groups present per molecule of the former compound is: (1) 5 (2) 4 (3) 6 (4) 2
Sol.	(1) $R - NH_2 + CH_3 - C - CI \longrightarrow R - NH - C - CH_3 + HC1$ Q_4 Each $CH_3 - C$ addition increases the molecular wt. by 42. Total increase in m.wt. = 390 - 180 = 210 Then number of NH_2 groups = $\frac{210}{42} = 5$
14.	Given $E^{0}_{C_{4}} = -0.74 \text{ V}; E^{0}_{MnO_{4}^{2}/Mn^{2+}} = 1.51 \text{ V}$ $E^{0}_{C_{2}} = 1.33 \text{ V}; E^{0}_{Cl/Cl^{-}} = 1.36 \text{ V}$ Based on the data given above, strongest oxidising agent will be: (1) Cr^{2+} (2) Mn^{2+} (3) MnO^{-}_{4} (4) Cl^{-}
Sol.	(3) As per data mentioned MnO_4^- is strongest oxidising agent as it has maximum SRP value.



[Co(NH₃)₃Cl₃] exists in two forms (facial and meridonial)



Both of these forms are achiral. Hence, [Co(NH₃)₃Cl₃] does not show optical isomerism.

19. A piston filled with 0.04 mol of an ideal gas expands reversibly from 50.0 mL to 375 mL at a constant temperature of 37.0°C. As it does so, it absorbs 208J of heat. The values of q and w for the process will be: (R = 8.314 J/mol K) (l n 7.5 = 2.01)

(n -	-0.51 + 571101 K/(cu /.5 - 2.01)
(1)	q = -208 J, w = -208 J
(3)	q = +208 J, w = +208 J

(2) q = -208 J, w = +208 J(4) q = +208 J, w = -208 J

Sol. (4)

Process is isothermal reversible expansion, hence $\Delta U = 0$. $\therefore q = -W$ As q = +208 JHence W = -208 J

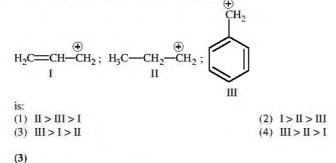
20. A gaseous hydrocarbon gives upon combustion 0.72 g of water and 3.08 g of CO₂. The empirical formula of the hydrocarbon is:

(1) C_3H_4	(2) C_6H_5
(3) C_7H_8	(4) C_2H_4

Sol. (3)

 $C_{x}H_{y} + \begin{cases} \frac{y}{2} \\ \frac{y}{4} \\ \frac{y}{4} \\ \frac{y}{6} \\ 0 \\ \frac{y}{4} \\ \frac{y}{6} \\ 0 \\ \frac{y}{2} \\ \frac$

21. The order of stability of the following carbocations:



Sol.

Order of stability is III > I > II.

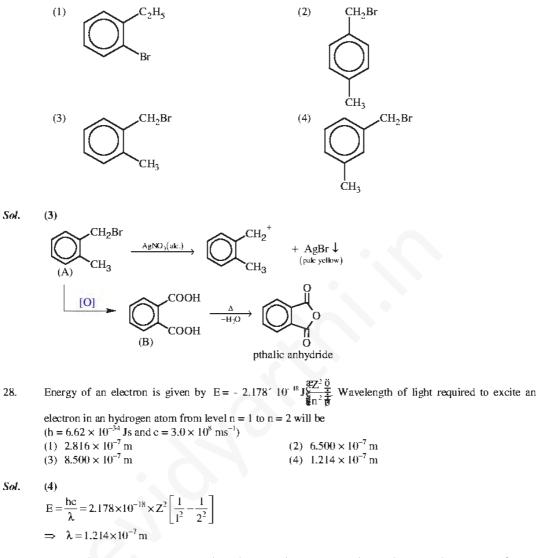
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- 22. Which of the following represents the correct order of increasing first ionization enthalpy for Ca, Ba, S, Se and Ar? (1) S < Se < Ca < Ba < Ar(2) Ba < Ca < Se < S < Ar(3) Ca < Ba < S < Se < Ar(4) Ca < S < Ba < Se < ArSol. (2)Increasing order of first ionization enthalpy is Ba < Ca < Se < S < Ar For gaseous state, if most probable speed is denoated by C^* , average speed by \overline{C} and mean square speed by 23. C, then for a large number of molecules the ratios of these speeds are: (1) $C^*:\overline{C}:C = 1.128:1.225:1$ (2) $C^*:\overline{C}:C = 1:1.128:1.225$ (3) $C^*:\overline{C}:C = 1:1.125:1.128$ (4) $C^*:\overline{C}:C = 1.225:1.128:1$ Sol. $C^* = \sqrt{\frac{2RT}{M}}$, $\overline{C} = \sqrt{\frac{8RT}{\pi M}}$, $C = \sqrt{\frac{3RT}{M}}$ The gas leaked from a storage tank of the Union Carbide plant in Bhopal gas tragedy was: 24. (1) Methylamine (2) Ammonia (3) Phosgene (4) Methylisocyanate Sol. (4) It was methyl isocyanate (CH₃NCO) 25. Consider the following reaction: $xMnO_4 + yC_2O_4^2 + zH^* \frac{3}{4} \frac{3}{2} xMn^{2*} + 2yCO_2 + \frac{z}{2}H_2O$ The values of x, y and z in the reaction are, respectively: (2) 2, 5 and 16 (1) 2, 5 and 8 (3) 5, 2 and 8 (4) 5, 2 and 16 Sol. (2) $2MnO_4^- + 5C_2O_4^{-2} + 16H^+ \longrightarrow 2Mn^{+2} + 10CO_2 + 8H_2O_2$ x = 2, y = 5, z = 16
 - Which of the following exists as covalent crystals in the solid state?
 (1) Silicon
 (2) Sulphur
 (3) Phosphorous
 (4) Iodine
 - Sol. (1)

 $\begin{array}{l} \mbox{Silicon} (Si) - \mbox{covalent solid} \\ \mbox{Sulphur} (S_8) - \mbox{molecular solid} \\ \mbox{Phosphorous} (P_4) - \mbox{Molecular solid} \\ \mbox{Iodine} (I_2) - \mbox{Molecular solid} \\ \mbox{Iodine} (I_2) - \mbox{Molecular solid} \\ \end{array}$

Compound (A), C₈H₉Br, gives a white precipitate when warmed with alcoholic AgNO₃. Oxidation of (A) gives a acid (B), C₈H₆O₄. (B) easily forms anhydride on heating. Identify the compound (A).



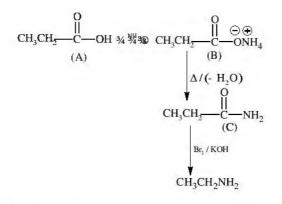


- 29. An organic compound A upon reacting with NH₃ gives B. On heating B gives C. C in presence of KOH reacts with Br₂ to give CH₃CH₂NH₂. A is

 (1) CH₃CH₂CH₂COOH
 (2) H₃C—CH—COOH
 - (3) CH₃CH₂COOH

(2) H₃C—CH—COOH
 I CH₃
 (4) CH₃COOH

Sol. (3)



30. In which of the following pairs of molecules/ions, both the species are not likely to exist? (1) $H^2 = Ha^{2}$ (2) $H^{24} = Ha^{24}$

(1) H_2^2 , He_2^2	(2)	$H_2^{2^+}$, He_2
(3) H_2^{-}, He_2^{2+}	(4)	H_2^+, He_2^{2}

Sol.

(2)

Bond order of H_2^{2+} and He_2 is zero, thus their existence is not possible.

PART B - MATHEMATICS

- 31. The circle passing through (1, -2) and touching the axis of x at (3, 0) also passes through the point (1)(2,-5)(2)(5, -2)(3)(-2,5)(4)(-5,2)
- Sol. (2) $(x-3)^2 + y^2 + \lambda y = 0$ The circle passes through (1, -2) $\Rightarrow 4 + 4 - 2\lambda = 0 \Rightarrow \lambda = 4$ $(x-3)^2 + y^2 + 4y = 0 \Rightarrow$ Clearly (5, -2) satisfies.
- 32. ABCD is a trapezium such that AB and CD are parallel and BC \perp CD. If \angle ADB = θ , BC = p and CD = q, then AB is equal to
 - (2) $\frac{p^2 + q^2}{p^2 \cos \theta + q^2 \sin \theta}$ (4) $\frac{\left(p^2 + q^2\right) \sin \theta}{p \cos \theta + q \sin \theta}$ (1) $\frac{p^2 + q^2 \cos \theta}{p \cos \theta + q \sin \theta}$ (3) $\frac{(p^2 + q^2)\sin\theta}{(p\cos\theta + q\sin\theta)^2}$

Given : A circle, $2x^2 + 2y^2 = 5$ and a parabola, $y^2 = 4\sqrt{5}x$. 33. **Statement – I**: An equation of a common tangent to these curves is $y = x + \sqrt{5}$.

Statement – II : If the line,
$$y = mx + \frac{\sqrt{5}}{m}$$
 (m $\neq 0$) is their common tangent, then m satisfies $m^4 - 3m^2 + 2 = 0$.

- Statement I is True; Statement -II is true; Statement-II is not a correct explanation for Statement-I (1)
- (2) Statement -I is True; Statement -II is False.
- (3)Statement -I is False; Statement -II is True
- (4) Statement -I is True; Statement -II is True; Statement-II is a correct explanation for Statement-I

Sol. (1)

Sol.

- Let the tangent to the parabola be $y = mx + \frac{\sqrt{5}}{m}$ (m $\neq 0$). Now, its distance from the centre of the circle must be equal to the radius of the circle. So, $\left|\frac{\sqrt{5}}{m}\right| = \frac{\sqrt{5}}{\sqrt{2}}\sqrt{1 + m^2} \implies (1 + m^2) m^2 = 2 \implies m^4 + m^2 2 = 0.$ \Rightarrow (m² - 1) (m² + 2) = 0 \Rightarrow m = ± 1 So, the common tangents are $y = x + \sqrt{5}$ and $y = -x - \sqrt{5}$.
- A ray of light along $x + \sqrt{3}y = \sqrt{3}$ gets reflected upon reaching x-axis, the equation of the reflected rays is 34.

(1)
$$\sqrt{3}y = x - \sqrt{3}$$

(2) $y = \sqrt{3}x - \sqrt{3}$
(3) $\sqrt{3}y = x - 1$
(4) $y = x + \sqrt{3}$

Sol. (1)

Slope of the incident ray is $-\frac{1}{\sqrt{3}}$.

So, the slope of the reflected ray must be $\frac{1}{\sqrt{3}}$.

The point of incidence is $(\sqrt{3}, 0)$. So, the equation of reflected ray is $y = \frac{1}{\sqrt{3}}(x - \sqrt{3})$.

35. All the students of a class performed poorly in Mathematics. The teacher decided to give grace marks of 10 to each of the students. Which of the following statistical measures will not change even after the grace marks were given ?

(1) median	(2) mode
(3) variance	(4) mean

Sol.

(3)

Variance is not changed by the change of origin. Alternate Solution:

$$\begin{split} \sigma &= \sqrt{\frac{\sum |\mathbf{x} - \overline{\mathbf{x}}|^2}{n}} \text{ for } \mathbf{y} = \mathbf{x} + 10 \Rightarrow \overline{\mathbf{y}} = \overline{\mathbf{x}} + 10 \\ \sigma_i &= \sqrt{\frac{\sum |\mathbf{y} + 10 - \overline{\mathbf{y}} - 10|^2}{n}} = \sqrt{\frac{\sum |\mathbf{y} - \overline{\mathbf{y}}|^2}{n}} = \sigma \;. \end{split}$$

- 36. If x, y, z are in A.P. and $\tan^{-1}x$, $\tan^{-1}y$ and $\tan^{-1}z$ are also in A.P., then (1) 2x = 3y = 6z (2) 6x = 3y = 2z(3) 6x = 4y = 3z (4) x = y = z
- Sol. (4) If x, y, z are in A.P. 2y = x + z

2y = x + zand $\tan^{-1}x$, $\tan^{-1}y$, $\tan^{-1}z$ are in A.P. $2\tan^{-1}y = \tan^{-1}x + \tan^{-1}z \implies x = y = z$. Note: If y = 0, then none of the options is appropriate.

37. If $\int f(x) dx = \Psi(x)$, then $\int x^5 f(x^3) dx$ is equal to (1) $\frac{1}{3}x^3\Psi(x^3) - 3\int x^3\Psi(x^3) dx + C$ (2) $\frac{1}{3}x^3\Psi(x^3) - \int x^2\Psi(x^3) dx + C$ (3) $\frac{1}{3}[x^3\Psi(x^3) - \int x^3\Psi(x^3) dx] + C$ (4) $\frac{1}{3}[x^3\Psi(x^3) - \int x^2\Psi(x^3) dx] + C$

$$(4^{3}) - \int x^{3} \Psi(x^{3}) dx + C$$

Sol.

(2)

$$\int_{1}^{1} f(x) dx = \psi(x)$$
Let $x^3 = t$

$$3x^2 dx = dt$$
then $\int x^5 f(x^3) dx = \frac{1}{3} \int tf(t) dt$

$$= \frac{1}{3} \left[t \int f(t) dt - \int \left\{ 1 \cdot \int f(t) dt \right\} dt \right] = \frac{1}{3} x^3 \psi(x^3) - \int x^2 \psi(x^3) dx + C.$$

- The equation of the circle passing through the foci of the ellipse $\frac{x^2}{16} + \frac{y^2}{9} = 1$, and having centre at (0, 3) is 38.
 - (1) $x^2 + y^2 6y + 7 = 0$ (2) $x^2 + y^2 - 6y - 5 = 0$ (3) $x^2 + y^2 - 6y + 5 = 0$ $(4) x^2 + y^2 - 6y - 7 = 0$

(4) foci \equiv (± ae, 0) We have $a^2e^2 = a^2 - b^2 = 7$ Equation of circle $(x - 0)^2 + (y - 3)^2 = (\sqrt{7} - 0)^2 + (0 - 3)^2$ $\Rightarrow x^2 + y^2 - 6y - 7 = 0.$

+by +cy

39. The x-coordinate of the incentre of the triangle that has the coordinates of mid points of its sides as (0, 1)(1, 1) and (1, 0) is

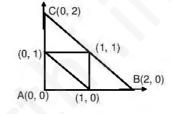
(1) $2 - \sqrt{2}$	(2) $1+\sqrt{2}$
(3) $1 - \sqrt{2}$	(4) $2+\sqrt{2}$

(1) Sol.

Sol.

x-coordinate =
$$\frac{4x_1 + 6x_2 + 6x_3}{a + b + c}$$

= $\frac{2 \times 2 + 2\sqrt{2} \times 0 + 2 \times 0}{2 + 2 + 2\sqrt{2}}$
= $\frac{4}{4 + 2\sqrt{2}} = \frac{2}{2 + \sqrt{2}} = 2 - \sqrt{2}$.
Alternate Solution:
x-coordinate = r = (s - a) tan A/2
= $\left(\frac{4 + 2\sqrt{2}}{2} - 2\sqrt{2}\right) \tan \frac{\pi}{4} = 2 - \sqrt{2}$



40. The intercepts on x-axis made by tangents to the curve, $y = \int |t| dt$, $x \in \mathbf{R}$, which are parallel to the line

y = 2x, are equal to	
$(1) \pm 2$	$(2) \pm 3$
(3) ±4	$(4) \pm 1$

Sol.

y

(4)

 $\frac{dy}{dx}$ |t| dt = 2 for x = 2 $=2 \Rightarrow x = \pm 2 =$ and $y = \int |t| dt = -2$ for x = -2: tangents are $y - 2 = 2(x - 2) \Rightarrow y = 2x - 2$ and $y + 2 = 2 (x + 2) \Rightarrow y = 2x + 2$ Putting y = 0, we get x = 1 and -1.

The sum of first 20 terms of the sequence 0.7, 0.77, 0.777,, is 41.

(1)
$$\frac{7}{9} \left(99 - 10^{-20}\right)$$

(2) $\frac{7}{81} \left(179 + 10^{-20}\right)$
(3) $\frac{7}{9} \left(99 + 10^{-20}\right)$
(4) $\frac{7}{81} \left(179 - 10^{-20}\right)$

Sol. (2) $t_r = 0.777 \dots r$ times

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$$= 7 (10^{-1} + 10^{-2} + 10^{-3} + \dots + 10^{-r})$$

= $\frac{7}{9} (1 - 10^{-r})$
 $S_{20} = \sum_{r=1}^{20} t_r = \frac{7}{9} \left(20 - \sum_{r=1}^{20} 10^{-r} \right) = \frac{7}{9} \left(20 - \frac{1}{9} (1 - 10^{-20}) \right) = \frac{7}{81} (179 + 10^{-20})$

42. Consider :

Statement – I : $(p \land \neg q) \land (\neg p \land q)$ is a fallacy.

- **Statement II :** $(p \rightarrow q) \leftrightarrow (\sim q \rightarrow \sim p)$ is a tautology.
- (1) Statement I is True; Statement -II is true; Statement-II is not a correct explanation for Statement-I
- (2) Statement -I is True; Statement -II is False.
- (3) Statement -I is False; Statement -II is True
- (4) Statement -I is True; Statement -II is True; Statement-II is a correct explanation for Statement-I

Sol. (1)

51.						
р	q	~p	~q	p^~q	~p^q	(p^~q)^(~p^q)
Т	Т	F	F	F	F	F
Т	F	F	Т	Т	F	F
F	Т	Т	F	F	Т	F
F	F	Т	Т	F	F	F
						Fallacy

S2:

JZ.						
р	q	~ p	~ q	p⇒q	~q⇒~p	$(p \Rightarrow q) \Leftrightarrow (\sim q \Rightarrow \sim p)$
Т	Т	F	F	Т	Т	Т
Т	F	F	Т	F	F	Т
F	Т	Т	F	Т	Т	Т
F	F	Т	Т	Т	Т	Т
						Tautology

S2 is not an explanation of S1

43. The area (in square units) bounded by the curves $y = \sqrt{x}$, 2y - x + 3 = 0, x-axis, and lying in the first quadrant is (1) 36 (2) 18

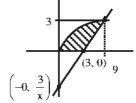
(4) 9

(1) 36 (3) $\frac{27}{4}$

Sol. (4)

$$2\sqrt{x} = x - 3$$

 $4x = x^2 - 6x + 9$
 $x^2 - 10x + 9$
 $x = 9, x = 1$
 $\int_{0}^{3} (2y+3) - y^2 dy$
 $\left[y^2 + 3y - \frac{y^3}{3} \right]_{0}^{3} = 9 + 9 - 9 = 9$



44. The expression $\frac{\tan A}{1-\cot A} + \frac{\cot A}{1-\tan A}$ can be written as (1) secA cosecA + 1 (2) tanA + cotA (3) secA + cosecA (4) sinA cosA + 1



$$\frac{1}{\cot A (1 - \cot A)} - \frac{\cot^2 A}{(1 - \cot A)} = \frac{1 - \cot^3 A}{\cot A (1 - \cot A)} = \frac{\cos ec^2 A + \cot A}{\cot A} = 1 + \sec A \csc A$$

- 45. The real number k for which the equation, $2x^3 + 3x + k = 0$ has two distinct real roots in [0, 1] (1) lies between 2 and 3 (3) does not exist (4) lies between 1 and 2
- Sol. (3) If 2x³ + 3x + k = 0 has 2 distinct real roots in [0, 1], then f' (x) will change sign but f'(x) = 6x² + 3 > 0 So no value of k exists.

46.
$$\lim_{x \to 0} \frac{(1 - \cos 2x)(3 + \cos x)}{x \tan 4x}$$
 is equal to
(1) $\frac{1}{2}$ (2) 1
(3) 2 (4) -

4) $-\frac{1}{4}$

Sol. (3)

$$\lim_{x \to 0} \frac{(1 - \cos 2x)}{x (\tan 4x)} (3 + \cos x)$$

$$\lim_{x \to 0} 2 \left(\frac{\sin x}{x} \right)^2 \cdot \frac{1}{4} \left(\frac{4x}{\tan 4x} \right) (3 + \cos x) = 2 \times 1 \times \frac{1}{4} \times 1 \times (3 + 1) = 2.$$

- 47. Let T_n be the number of all possible triangles formed by joining vertices of an n-sided regular polygon. If $T_{n+1} T_n = 10$, then the value of n is (1) 5 (2) 10 (4) 7
- Sol. (1) ${}^{n+1}C_3 - {}^nC_3 = 10 \Rightarrow {}^nC_2 = 10 \Rightarrow n = 5.$

48.

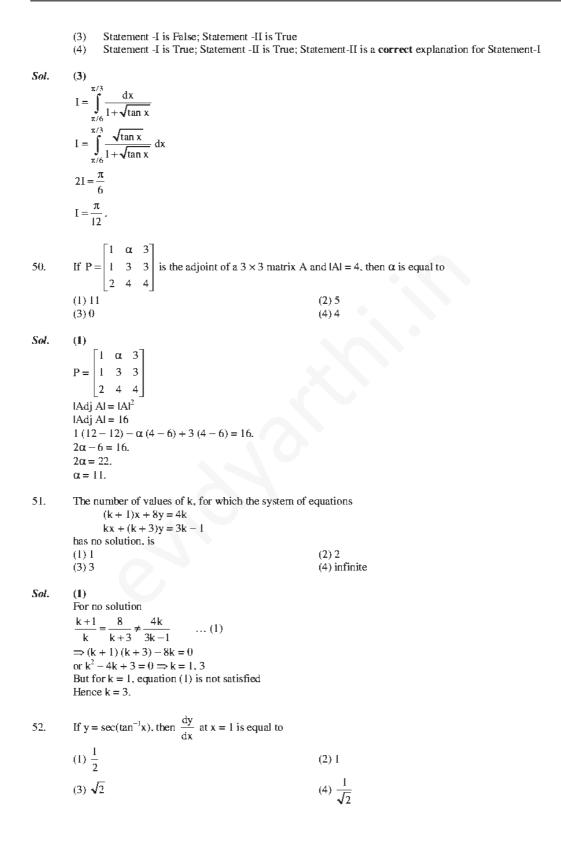
At present, a firm is manufacturing 2000 items. It is estimated that the rate of change of production P w.r.t. additional number of workers x is given by $\frac{dP}{dx} = 100 - 12\sqrt{x}$. If the firm employs 25 more workers, then the new level of production of items is

the new level of production of items	0
(1) 3000	(2) 3500
(3) 4500	(4) 2500

- Sol. (2) $\int_{2000}^{P} dP = \int_{0}^{25} (100 - 12\sqrt{x}) dx$ $(P - 2000) = 25 \times 100 - \frac{12 \times 2}{3} (25)^{3/2}$ P = 3500.
- 49. Statement I: The value of the integral $\int_{x/6}^{x/3} \frac{dx}{1 + \sqrt{\tan x}}$ is equal to $\frac{\pi}{6}$. Statement – II: $\int_{0}^{b} f(x) dx = \int_{0}^{b} f(a+b-x) dx$.
 - (1) Statement I is True; Statement -II is true; Statement-II is not a correct explanation for Statement-I
 - (2) Statement -I is True; Statement -II is False.



JEE (MAIN)-2013-CMP-15



Sol. (4) $y = \sec(\tan^{-1}x)$ $\frac{dy}{dx} = \sec\left(\tan^{-t} x\right) \tan\left(\tan^{-t} x\right) \cdot \frac{1}{1+x^2}$ $\frac{\mathrm{dy}}{\mathrm{dx}}\Big|_{x=1} = \sqrt{2} \times 1 \times \frac{1}{2} = \frac{1}{\sqrt{2}}.$ If the lines $\frac{x-2}{1} = \frac{y-3}{1} = \frac{z-4}{-k}$ and $\frac{x-1}{k} = \frac{y-4}{2} = \frac{z-5}{1}$ are coplanar, then k can have (1) exactly one value (2) exactly two values 53. (3) exactly three values (4) any value Sol. (2) -1 -1 -k = 02 $1(1+2k) + 1(1+k^2) - 1(2-k) = 0$ $k^2 + 1 + 2k + 1 - 2 + k = 0$ $k^2 + 3k = 0$ (k)(k+3) = 02 values of k. 54. Let A and B be two sets containing 2 elements and 4 elements respectively. The number of subsets of A × B having 3 or more elements is (2) 219(1)220(4) 256 (3) 211 Sol. (2)A × B will have 8 elements. $2^8 - {}^8C_0 - {}^8C_1 - {}^8C_2 = 256 - 1 - 8 - 28 = 219.$ If the vectors $\overrightarrow{AB} = 3\hat{i} + 4\hat{k}$ and $\overrightarrow{AC} = 5\hat{i} - 2\hat{j} + 4\hat{k}$ are the sides of a triangle ABC, then the length of the 55. median through A is (2) $\sqrt{33}$ (4) $\sqrt{18}$ (1) √72 (3) √45 Sol. (2) $\overline{AM} = \frac{\overline{AB} + \overline{AC}}{2}$ $\overrightarrow{AM} = 4\hat{i} - \hat{j} + 4\hat{k}$ $\left|\overline{\mathrm{AM}}\right| = \sqrt{16 + 16 + 1} = \sqrt{33}$ R 56. A multiple choice examination has 5 questions. Each question has three alternative answers of which exactly one is correct. The probability that a student will get 4 or more correct answers just by guessing is (1) $\frac{13}{3^5}$ (2) $\frac{11}{3^5}$ (3) $\frac{10}{3^5}$ (4) $\frac{17}{3^5}$ (2)

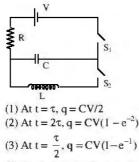
Sol.

P (correct answer) = 1/3

 ${}^{5}C_{4}\left(\frac{1}{3}\right)^{4}\left(\frac{2}{3}\right)^{1} + {}^{5}C_{5}\left(\frac{1}{3}\right)^{5}$ $\frac{5\times 2}{(3)^5} + \frac{1}{(3)^5} = \frac{11}{3^5}.$ If z is a complex number of unit modulus and argument θ , then $\arg\left(\frac{1+z}{1+z}\right)$ equals 57. (1) $\frac{\pi}{2} - \theta$ (2) 0 (3) $\pi - \theta$ $(4) - \theta$ Sol. (2) $|z| = 1 \implies z\overline{z} = 1$ $\frac{1+z}{1+\overline{z}} = \frac{1+z}{1+\frac{1}{2}} = z \; .$ 58. If the equations $x^2 + 2x + 3 = 0$ and $ax^2 + bx + c = 0$, $a, b, c \in \mathbb{R}$, have a common root, then a:b:cis (1)3:2:1(2) 1 : 3 : 2 (3) 3:1:2 (4) 1:2:3 Sol. (4) For equation $x^2 + 2x + 3 = 0$ both roots are imaginary. Since $a, b, c \in R$. If one root is common then both roots are common Hence, $\frac{a}{1} = \frac{b}{2} = \frac{c}{3}$ a:b:c=1:2:3.59. Distance between two parallel planes 2x + y + 2z = 8 and 4x + 2y + 4z + 5 = 0 is (1) $\frac{5}{2}$ (2) $\frac{7}{2}$ $(4)\frac{3}{2}$ (3) $\frac{9}{2}$ Sol. (2) 4x + 2y + 4z = 164x + 2y + 4z = -5 $d_{\min} = \frac{21}{\sqrt{36}} = \frac{21}{6} = \frac{7}{2}.$ The term independent of x in expansion of $\left(\frac{x+l}{x^{2/3}-x^{1/3}+l}-\frac{x-l}{x-x^{1/2}}\right)^{l0}$ is 60. (1) 120(2) 210(3) 310 (4)4Sol. (2) $\left(\frac{\left(x^{1/3}+1\right)\left(x^{2/3}-x^{1/3}+1\right)}{x^{2/3}-x^{1/3}+1}-\frac{1}{\sqrt{x}}\cdot\frac{\left(\sqrt{x}+1\right)\left(\sqrt{x}-1\right)}{\left(\sqrt{x}-1\right)}\right)^{10}=(x^{1/3}-x^{-1/2})^{10}$
$$\begin{split} T_{r+1} &= (-1)^{r-10} C_r \ x^{\frac{20-5r}{6}} \implies r = 4 \\ {}^{10}C_4 &= 210. \end{split}$$

PART C - PHYSICS

61. In an LCR circuit as shown below both switches are open initially. Now switch S₁ is closed, S₂ kept open. (q is charge on the capacitor and $\tau = RC$ is capacitive time constant). Which of the following statement is correct?



(4) Work done by the battery is half of the energy dissipated in the resistor.

```
Sol.
         (2)
```

Charge on the capacitor at any time 't' is $q = CV(1-e^{-t/\tau})$ at $t = 2\tau$ $q = CV(1 - e^{-2})$

- 62. A diode detector is used to detect an amplitude modulated wave of 60% modulation by using a condenser of capacity 250 pico farad in parallel with a load resistance 100 kilo ohm. Find the maximum modulated frequency which could be detected by it. (1) 10.62 kHz (2) 5.31 MHz (3) 5.31 kHz (4) 10.62 MHz
- Sol. (3)

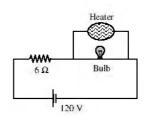
= 6.37 kHz $f_{C} =$ $2\pi RC$ 2×3.14×100×10³×250×10 $f_{C} = cut off frequency$ As we know that $f_m \square f_C$:. (3) is correct Note: The maximum frequency of modulation must be less than f_m , where $f_m = f_C \frac{\sqrt{1 - m^2}}{\sqrt{1 - m^2}}$ m $m \Rightarrow modulation index$

63. The supply voltage to a room is 120 V. The resistance of the lead wires is 6 Ω . A 60 W bulb is already switched on. What is the decrease of voltage across the bulb, when a 240 W heater is switched on in parallel to the bulb? (1) 2.9 Volt (2) 13.3 Volt (4) zero volt

(3) 10.04 Volt

Sol. (3)

Resistance of bulb = $\frac{120 \times 120}{60} = 240\Omega$ Resistance of Heater = $\frac{120 \times 120}{240} = 60\Omega$



Voltage across bulb before heater is switched on, $V_1 = \frac{120}{246} \times 240$ Voltage across bulb after heater is switched on, $V_2 = \frac{120}{54} \times 48$

Decrease in the voltage is $V_1 - V_2 = 10.04$ (approximately) Note: Here supply voltage is taken as rated voltage.

64. A uniform cylinder of length L and mass M having cross-sectional area A is suspended, with its length vertical, from a fixed point by a massless spring, such that it is half submerged in a liquid of density σ at equilibrium position. The extension x_0 of the spring when it is in equilibrium is:

(1) $\frac{Mg}{k} \left(1 - \frac{LA\sigma}{M} \right)$	(2) $\frac{Mg}{k} \left(1 - \frac{LA\sigma}{2M} \right)$
(3) $\frac{Mg}{k} \left(1 + \frac{LA\sigma}{M} \right)$	(4) $\frac{Mg}{k}$
(Here k is spring constant)	

Sol. (2)

At equilibrium
$$\Sigma F = 0$$

 $kx_0 + \left(\frac{AL}{2}\sigma g\right) - Mg = 0$
 $x_0 = Mg \left[1 - \frac{LA\sigma}{2M}\right]$

Buoyant force

65. Two charges, each equal to q, are kept at x = -a and x = a on the x-axis. A particle of mass m and charge $q_0 = \frac{q}{2}$ is placed at the origin. If charge q_0 is given a small displacement (y \square a) along the y-axis, the net force acting on the particle is proportional to:

(1)
$$-y$$

(3) $-\frac{1}{y}$
(4) y

Sol.

(4)

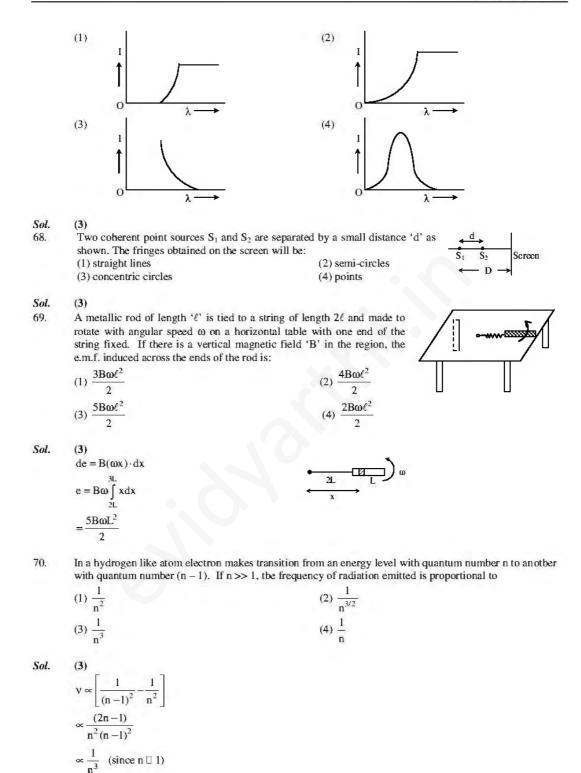
$$F_{net} = 2F\cos\theta$$

$$= 2\frac{k \cdot q \cdot q/2}{\left(\sqrt{a^2 + y^2}\right)^2} \cdot \frac{y}{\sqrt{a^2 + y^2}}$$

$$= \frac{kq^2y}{a^3} (y \square a)$$

- 66. A beam of unpolarised light of intensity I₀ is passed through a polaroid A and then through another polaroid B which is oriented so that its principal plane makes an angle of 45° relative to that of A. The intensity of the emergent light is:

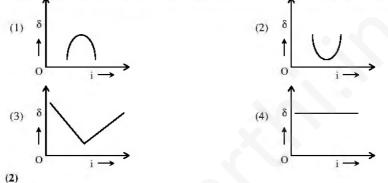
 (1) I₀/2
 (2) I₀/4
 (3) I₀/8
 (4) I₀
- Sol. (2)
- 67. The anode voltage of a photocell is kept fixed. The wavelength λ of the light falling on the cathode is gradually changed. The plate current I of the photocell varies as follows:



Educational Material Downloaded from http://www.evidyarthi.in/ Get CBSE Notes, Video Tutorials, Test Papers & Sample Papers 71. Assume that a drop of liquid evaporates by decrease in its surface energy, so that its temperature remains unchanged. What should be the minimum radius of the drop for this to be possible? The surface tension is T, density of liquid is p and L is its latent heat of vaporization.

(1) $\sqrt{\Gamma/\rho L}$ (3) $2T/\rho L$ (3) $2T/\rho L$ (4) $\rho L/T$ Sol. (3) $\rho 4\pi R^2 \Delta RL = T 4\pi [R^2 - (R - \Delta R)^2]$ $\rho R^2 \Delta RL = T[R^2 - R^2 + 2R\Delta R - \Delta R^2]$ $\rho R^2 \Delta RL = T2R\Delta R (\Delta R \text{ is very small})$ $R = \frac{2T}{\rho L}$.

72. The graph between angle of deviation (δ) and angle of incidence (i) for a triangular prism is represented by:



- Sol. (2)
- 73. Let $[\varepsilon_0]$ denote the dimensional formula of the permittivity of vacuum. If M = mass, L = length, T = time and A = electric current, then: $(1) <math>[\varepsilon_0] = [M^{-1}L^{-3}T^{4}A^{2}]$ (2) $[\varepsilon_0] = [M^{-1}L^{2}T^{-1}A^{-2}]$ (3) $[\varepsilon_0] = [M^{-1}L^{2}T^{-1}A]$ (4) $[\varepsilon_0] = [M^{-1}L^{-3}T^{2}A]$
- Sol. (1)

$$\frac{1}{4\pi\epsilon_0} \frac{q}{r^2} = F$$

$$\epsilon_0 = \frac{[A^2T^2]}{[M]T^{-2}T^2]} = [M^{-1}L^{-3}A^2T^4]$$

74.

73.

 $\begin{array}{c}
\uparrow & 2p_0 \\
P & p_0 \\
O & D \\
V_0 & 2v_0
\end{array}$

The above p-v diagram represents the thermodynamic cycle of an engine, operating with an ideal monoatomic gas. The amount of heat extracted from the source in a single cycle is

$(1)\left(\frac{13}{2}\right)\mathbf{p}_0\mathbf{v}_0$	(2) $\left(\frac{11}{2}\right) \mathbf{p}_0 \mathbf{v}_0$
$(3) 4p_0v_0$	(4) $p_0 v_0$

Sol.

(2)

Heat is extracted from the source in path DA and AB is

$$\Delta Q = \frac{3}{2} R \left(\frac{P_0 V_0}{R} \right) + \frac{5}{2} R \left(\frac{2 P_0 V_0}{R} \right) = \frac{13}{2} P_0 V_0$$

75. A sonometer wire of length 1.5 m is made of steel. The tension in it produces an elastic strain of 1 %. What is the fundamental frequency of steel if density and elasticity of steel are 7.7×10^3 kg/m³ and 2.2×10^{11} N/m² respectively? (2) 200.5 Hz (1) 178.2 Hz (3) 770 Hz

(4) 188.5 Hz

Sol. (1)

Fundamental frequency
$$f = \frac{1}{2\ell} \sqrt{\frac{T}{\mu}}$$

= $\frac{1}{2\ell} \sqrt{\frac{T}{A\rho}}$
= $\frac{1}{2\ell} \sqrt{\frac{stress}{\rho}} = \frac{1}{2\times 15} \sqrt{\frac{2.2 \times 10^{11} \times 10}{7.7 \times 10^3}}$

This question has statement I and statement II. Of the four choices given after the statements, choose the 76. one that best describes the two statements.

Statement- I: Higher the range, greater is the resistance of ammeter.

-2

Statement- II: To increase the range of ammeter, additional shunt needs to be used across it.

- (1) Statement I is true, Statement II is true, Statement II is not the correct explanation of Statement-L
- (2) Statement I is true, statement II is false.

(3) Statement - I is false, Statement - II is true

(4) Statement - I is true, Statement - II is true, Statement - II is the correct explanation of statement- I.

Sol. (3)

For Ammeter, $S = \frac{I_g G}{1 - I_g}$

So for I to increase, S should decrease, so additional S can be connected across it.

77. What is the minimum energy required to launch a satellite of mass m from the surface of a planet of mass M and radius R in a circular orbit at an altitude of 2R?

(1) $\frac{2\text{GmM}}{1}$	(2) GmM
$\frac{(1)}{3R}$	(2) 2R
(3) \underline{GmM}	(4) $\frac{5 \text{GmM}}{1000}$
(3) $\overline{3R}$	(4) 6R

Sol. (4)

> GMm T. $E_f =$ 6R GMm T. $E_i = \Delta W = T.E_f - T.E_i = \frac{5GMm}{c_T}$

A projectile is given an initial velocity of $(\hat{i}+2\hat{j})$ m/s, where \hat{i} is along the ground and \hat{j} is along the 78. vertical. If $g = 10 \text{ m/s}^2$, the equation of its trajectory is:

(1) $y = 2x - 5x^2$	(2) $4y = 2x - 5x^2$
(3) $4y = 2x - 25x^2$	(4) $y = x - 5x^2$

Sol. (1) x = ty = 2t - 5t² Equation of trajectory is $y = 2x - 5x^{2}$

79. Two capacitors C_1 and C_2 are charged to 120 V and 200 V respectively. It is found that by connecting them together the potential on each one can be made zero. Then :

(1) $3C_1 = 5C_2$	(2)	$3C_1 + 5C_2 = 0$
(3) $9C_1 = 4C_2$	(4)	$5C_1 = 3C_2$

Sol. (1) $120C_1 = 200C_2$ $6C_1 = 10C_2$

 $3C_1 = 5C_2$

80. A hoop of radius r and mass m rotating with an angular velocity a_0 is placed on a rough horizontal surface. The initial velocity of the centre of the hoop is zero. What will be the velocity of the centre of the hoop when it ceases to slip?

(1) $\frac{r\omega_b}{3}$	(2)	$\frac{r\omega_0}{2}$
(3) $r\omega_0$	(4)	$\frac{r\omega_0}{4}$

Sol.

(2)

From conservation of angular momentum about any fix point on the surface $mr^2\omega_0 = 2mr^2\omega$

$$\therefore \quad \omega = \frac{\omega_0}{2}$$
$$\therefore \quad V_{CM} = \frac{\omega_0 r}{2}$$

81.

Sol.

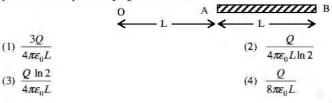
An ideal gas enclosed in a vertical cylindrical container supports a freely moving piston of mass M. The piston and cylinder have equal cross sectional area A. When the piston is in equilibrium, the volume of the gas is V_0 and its pressure is P_0 . The piston is slightly displaced from the equilibrium position and released. Assuming that the system is completely isolated from its surrounding, the piston executes a simple harmonic motion with frequency:

	(1) $\frac{1}{2\pi} \frac{V_0 M P_0}{A^2 \gamma}$	(2) $\frac{1}{2\pi}\sqrt{\frac{A^2\gamma P_0}{MV_0}}$
$P_{abc}A$ $P_{0}A$		(4) $\frac{1}{2\pi} \frac{A\gamma P_0}{V_0 M}$
FBD of piston at equilibrium $\Rightarrow P_{atm} A + mg = P_0 A \qquad(1)$		
$\Rightarrow P_{atm} A + mg = P_0 A \qquad(1)$		
	FBD of piston at equilibrium	
	\Rightarrow P _{atm} A + mg = P ₀ A	(1)
$(P_{0+}dP)A$	Pate A	
mg		
FBD of piston when piston is pushed down a distance x		wn a distance x

$$P_{atm} + mg - (P_0 + dP) A = m \frac{d^2 x}{dt^2} \qquad ...(2)$$

Process is adiabatic $\Rightarrow PV^{\gamma} = C \Rightarrow -dP = \frac{\gamma P dV}{V}$
Using 1, 2, 3 me get $f = \frac{1}{2\pi} \sqrt{\frac{A^2 \gamma P_0}{MV_0}}$

82. A charge Q is uniformly distributed over a long rod AB of length L as shown in the figure. The electric potential at the point O lying at a distance L from the end A is:



Sol.

(3)

(4)

$$V = \int_{x=L}^{x=2L} \frac{k}{x} \left(\frac{Q}{L}\right) dx = \frac{Q \ln 2}{4\pi\varepsilon_0 L}$$

- 83. A circular loop of radius 0.3 cm lies parallel to a much bigger circular loop of radius 20 cm. The centre of the small loop is on the axis of the bigger loop. The distance between their centres is 15 cm. If a current of 2.0 A flows through the smaller loop, then the flux linked with bigger loop is (1) 6×10^{-11} weber (2) 3.3×10^{-11} weber (3) 6.6×10^{-9} weber (4) 9.1×10^{-11} weber
- Sol.

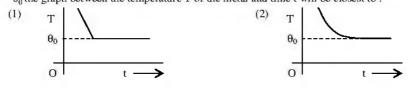
Let M_{12} be the coefficient of mutual induction between loops $\phi_1 = M_{12}i_2$

$$\Rightarrow \frac{\mu_0 i_2 R^2}{2(d^2 + R^2)^{3/2}} \pi r^2 = M_{12} i_2$$

$$\Rightarrow M_{12} = \frac{\mu_0 R^2 \pi r^2}{2(d^2 + R^2)^{3/2}}$$

$$\phi_2 = M_{12} i_1 \Rightarrow \phi_2 = 9.1 \times 10^{-11} \text{ weber}$$

84. If a piece of metal is heated to temperature θ and then allowed to cool in a room which is at temperature θ_0 the graph between the temperature T of the metal and time t will be closest to :



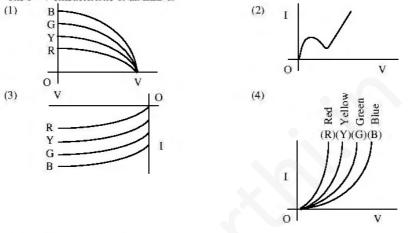
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Sol. (2)

The temperature goes on decreasing with time (non-linearly) The rate of decrease will be more initially which is depicted in the second graph.

85. The I – V characteristic of an LED is



Sol.

(4)

For LED, in forward bias, intensity increases with voltage.

86. This question has Statement I and Statement II. Of the four choices given after the Statements, choose the one that best describes the two Statements.

Statement – I: A point particle of mass m moving with speed v collides with stationary point particle of mass M. If the maximum energy loss possible is given as $f\left(\frac{1}{2}mv^2\right)$ then $f = \left(\frac{m}{M+m}\right)$.

mass M. If the maximum energy loss possible is given as $\int \left(\frac{1}{2}mv\right)^{1/2} dv = \left(\frac{1}{M+m}\right)^{1/2}$. Statement – II : Maximum energy loss occurs when the particles get stuck together as a result of the

collision.

(1) Statement - I is true, Statement - II is true, Statement - II is not a correct explanation of Statement - I.

(2) Statement - I is true, Statement - II is false.

(3) Statement - I is false, Statement - II is true

- (4) Statement I is true, Statement II is true, Statement II is a correct explanation of Statement I.
- Sol. (3)

Loss of energy is maximum when collision is inelastic as in an inelastic collision there will be maximum deformation.

KE in COM frame is
$$\frac{1}{2} \left(\frac{Mm}{M+m} \right) V_{rel}^2$$

KE_i = $\frac{1}{2} \left(\frac{Mm}{M+m} \right) V^2$ KE_f = 0 ($\because V_{rel} = 0$)
Hence loss in energy is $\frac{1}{2} \left(\frac{Mm}{M+m} \right) V^2$
M

$$\Rightarrow f = \frac{1}{M+1}$$

m

87. The amplitude of a damped oscillator decreases to 0.9 times its original magnitude is 5s. In another 10s it will decrease to α times its original magnitude, where α equals. (1) 0.81
(2) 0.729
(3) 0.6
(4) 0.7

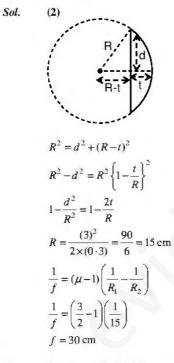
Sol. (2)

 $A = A_0 e^{-kt}$ $\Rightarrow 0.9A_0 = A_0 e^{-5k}$ and $\alpha A_0 = A_0 e^{-15k}$ solving $\Rightarrow \alpha = 0.729$

88. Diameter of plano-convex lens is 6 cm and thickness at the centre is 3 mm. If speed of light in material of lens is 2×10^8 m/s, the focal length of the lens is :

(2) 30 cm(4) 15 cm

	0	
(1) 20 cm		
(3) 10 cm		



89. The magnetic field in a travelling electromagnetic wave has a peak value of 20 nT. The peak value of electric field strength is :

(1) 6 V/m	(2) 9 V/n
(3) 12 V/m	(4) 3 V/n

Sol.

(

(1)

 $E_0 = CB_0$ = 3 × 10⁸ × 20 × 10⁻⁹ = 6 V/m

90. Two short bar magnets of length 1 cm each have magnetic moments 1.20 Am^2 and 1.00 Am^2 respectively. They are placed on a horizontal table parallel to each other with their N poles pointing towards the South. They have a common magnetic equator and are separated by a distance of 20.0 cm. The value of the resultant horizontal magnetic induction at the mid - point O of the line joining their centres is close to (Horizontal component of earth's magnetic induction is $3.6 \times 10^{-5} \text{ Wb/m}^2$)

(1) $2.56 \times 10^{-4} \text{ Wb/m}^2$ (3) $5.80 \times 10^{-4} \text{ Wb/m}^2$ Sol. (1) $B_{net} = B_{M_1} + B_{M_2} + B_H$ $\begin{aligned} B_{net} &= B_{M_1} + B_{M_2} + B_H \\ &= \frac{\mu_0 M_1}{4\pi x^3} + \frac{\mu_0 M_2}{4\pi x^3} + B_H \\ &= \frac{\mu_0}{4\pi x^3} (M_1 + M_2) + B_H \\ &= \frac{10^{-7}}{10^{-3}} \times 2.2 + 3.6 \times 10^{-5} \end{aligned}$ $= 2.56 \times 10^{-4}$ Wb/m²

- (2) $3.50 \times 10^{-4} \text{ Wb/m}^2$ (4) $3.6 \times 10^{-5} \text{ Wb/m}^2$