IT-JEE2005-PH-1

Solutions to IITJEE-2005 Mains Paper

Physics

Time: 2 hours

- Note: Question number 1 to 8 carries 2 marks each, 9 to 16 carries 4 marks each and 17 to 18 carries 6 marks each
- D1 A whisiting train approaches a junction. An observer standing at junction observes the frequency to be 22 KHz and 1.8 KHz of the approaching and the receding train. Find the speed of the train (speed of sound = 300 m/s)
- Sol. While approaching

$$t' = t_0 \left(\frac{v}{v - v_s} \right)$$
$$2200 = t_0 \left(\frac{300}{300 - v_s} \right)$$

While receding

$$I^* = f_0 \left(\frac{v}{v + v_s} \right)$$

$$1800 = f_0 \left(\frac{300}{300 + v_s} \right)$$

On solving velocity of source (train) v₄ = 30 m/s

- D2 A conducting liquid bubble of radius a and thickness t (t << a) is charged to patential V. If the bubble collapses to a droplet, find the potential on the droplet.</p>
- Sol. Potential of the bubble $(V) = \frac{1}{4\pi\epsilon_0} \frac{q}{s}$

by conservation of volume

$$4\pi a^{2}t = \frac{9}{3}\pi R^{3}$$

 $R = (3a^{2}t)^{12}$

Hence, potential on the droplet

$$V^{i} = \frac{1}{4\pi s_{D}} \frac{q}{R}$$
 (as charge is conserved)
 $\Rightarrow V^{i} = \left(\frac{a}{31}\right)^{V^{2}} V$

D3 The potential energy of a particle of mass m is given by

$$I(8) = \begin{cases} E_0 & 0 \le x \le 1 \\ 0 & \Rightarrow x = 1 \end{cases}$$

λ, and λ₂ are the de-Broglie wavelengths of the particle, when 0.5 × 5.1 and × + 1 respectively. If the total energy of particleducational Material Downloaded from http://www.evidyarthi.in/ Get CBSE Notes, Video Tutorials, Test Papers & Sample Papers



(tor 0 5 2 5 1)

(tor k > 1)

Sol. K.E. =
$$2E_0 - E_0 = E_0$$

 $\lambda_1 = \frac{h}{\sqrt{2mE_0}}$
 $KE = 2E_0$
 $\lambda_2 = \frac{h}{\sqrt{4mE_0}}$

$$\frac{\lambda_1}{\lambda_2} = \sqrt{2}$$

IQ4 A Li tube is rotated about one of it's limbs with an angular velocity ∞. Find the difference in height H of the liquid (density ρ) level, where diameter of the tube d << L.</p>



Sol.
$$\Delta PA = \int_{0}^{L} dm ccc^{2}$$

 $\rho gHA = \frac{c^{2}L^{2}\rho A}{2}$
 $H = \frac{L^{2}cc^{2}}{2\rho}$





Sol Apply conservation of angular momentum about O

$$(mv)L = (mL2 + \frac{ML^2}{3})to$$
$$to = \frac{3mv}{(3m + M)L}$$

Q8. What will be the minimum angle of incidence such that the total internal reflection occurs on both the surfaces?

Sol. For first surface 2 sinc, = √2 sin90* ⇒ c, = 45° For second surface 2 sincy= √3 sin90* ⇒ cy= 60*

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The side of a cube is measured by vernier callipers (10 divisions of a vernier scale coincide with 07 9 divisions of main scale, where 1 division of main scale is 1 mm). The main scale reads 10 mm and first division of vernier scale coincides with the main scale. Mars of the cube is 2 736 g. Find the density of the cube in appropriate significant figures.

Sol. Least count of vernier callipers =
$$(1 - \frac{9}{10})$$
mm = 0.1mm
Side of the cube = 10 mm + 1 = 0.1 mm = 10.1 mm = 1.01 cm

Density =
$$\frac{2730}{(1.01)^3} = 2.66 \text{g/cm}^3$$

06. An unknown resistance X is to be determined using resistances R., R. or R., Their corresponding null points are A, B and C. Find which of the above will give the most acourate reading and why?



$$\frac{\delta X}{X} = \frac{\delta r_1}{r_1} + \frac{\delta r_2}{r_2}$$

$$\frac{\delta r_1}{X} = \frac{\delta r_2}{r_2} = \frac{\delta X}{r_2}$$

to be minimum, No.

should be maximum and as 1, + 1, is constant.

This is true for h - 12. So R₂ gives most accurate value.

- 03 A transverse harmonic disturbance is produced in a string. The maximum transverse velocity is 3 m/s and maximum transverse acceleration is 90 m/s". If the wave velocity is 20 m/s then find the waveform.
- If amplitude of wave is A and angular frequency is to Sol.

$$\frac{\omega A}{\omega^2 A} = \frac{3}{90} \Rightarrow \qquad \omega = 30 \text{ rad/s}$$

$$v = \frac{\omega}{k} \qquad \Rightarrow \qquad k = \frac{3}{2} \text{m}^2$$

A= 10 cm

Considering sinusoidal harmonic function

.
$$y = (10 \text{ om}) \sin(30t \pm \frac{3}{2} + \phi)$$

A cylinder of mass m and radius R rolls down an inclined plane of inclination 8. Calculate the linear Q 10. acceleration of the axis of cylinder.

Sol. mgsinθ-f = ma_{sule} (1)
fR = l_{axis}
$$\alpha$$
. (2)
 $a_{axis} = R\alpha$. (3)
 $a_{axis} = \frac{2gs(n8)}{3}$

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Q11. A long solenoid of radius a and number of turns per unit length n is enclosed by cylindrical shell of radius R, thickness d (d<<R) and length L A variable current i = is in cot flows through the coil. If the resistivity of the material of cylindrical shell is p, find the induced current in the shell.







Sol. \$= (µonig since) na

- Q12. Two identical ladders, each of mass M and length L are resting on the rough horizontal surface as shown in the figure. A block of mass m hangs from P. If the system is in equilibrium, find the magnitude and the direction of frictional force at A and B.
- Sol. For equilibrium of whole system.

$$\Sigma F_v = 0$$

 $\approx N_m \left(\frac{2M + m}{m}\right)$

For rotational equilibrium of either ladder Calculating lorgue about P

NL cos
$$\theta = Mg \frac{L}{2} \cos \theta = \pi \sin \theta = 0$$

 $t = (M+m)g \frac{\cot \theta}{2}$

Q13. Highly energetic electrons are bombarded on a target of an element containing 30 neutrons. The tatio of radii of nucleus to that of Helium nucleus is (14)⁴⁴ Find

- (a) atomic number of the nucleus
- (b) the frequency of K, line of the X-ray produced. ($R = 1.1 \times 10^{7} \text{ m}^{2}$ and $e = 3 \times 10^{8} \text{ m/s}$)

⇒ A = 56 and Z = (56 - 30) = 26 for K_-line.

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IT-JEE2005-PH-5

Q14. A small body attached to one end of a vertically hanging spring is performing SHM about it's mean position with angular frequency and amplitude a. If at a height y" from the mean position the body gets detached from the spring, calculate the value of y" so that the height H attained by the mass is maximum. The body does not interact with the spring during its subsequent motion after detachment. (abo > g)

Sol At position B as the potential energy of the spring will be zero, the total energy (Gravitational potential energy + Kinetic energy) of the block at this point will be maximum and therefore if the block gets detached at this point, it will rise to maximum height.

$$y^{*} = \frac{mg}{k} - \frac{g}{\omega^{2}} < a$$



Q15. In the given circuit, the switch S is closed at time t = 0. The charge Q on the capacitor at any instant1 is given by Q(t) = Q₀ (1-e^{-b}). Find the value of Q₀ and **G** in terms of given parameters shown in the circuit.

Sol. Applying KVL in loop 1 and 2,

$$V = \frac{1}{R} - \frac{q}{C} = 0 \qquad (1)$$

$$\frac{q}{C} - \frac{1}{2}R_{c} = 0 \qquad (2)$$

$$\frac{1}{L} - \frac{1}{2} = \frac{dq}{dt} \qquad (3)$$

On solving we get

att.

$$q = \frac{CVR_2}{R_1 + R_2} \left(1 - e^{\frac{KR_1 + R_2}{CR_1 + R_2}} \right)$$

= $G_0 = \frac{CVR_2}{R_1 + R_2}$ and $\alpha = \frac{R_1 + R_2}{CR_1 + R_2}$

QIB.

- Two identical prisms of refractive index 13 are kept as shown in the figure. A light ray strikes the first prism at face AB. Find,
 - (a) the angle of incidence, so that the emergent ray from the first prism has minimum deviation.
 - (b) through what angle the prism DCE should be rotated about C so that the final emergent lay also has minimum deviation.

Sol. (a) For minimum deviation

$$r_1 = r_2 = \frac{10}{2}$$

$$\frac{\sin 1}{\sin 30^2} = \sqrt{3}$$

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(b) Prism DCE should be rotated about C in anticlockwise direction through 60° so that the final emergent ray "Educational Material Downloaded from http://www.evidyarthi.m/? uminimum) Get CBSE Notes, Video Tutorials, Test Papers & Sample Papers







IT-JEE2005-PH-6

Q17. A cylinder of mass 1 kg is given heat of 2000CU at atmospheric pressure. If initially temperature of cylinder is 20°C, find

(a) final temperature of the cylinder.

- (b) work done by the cylinder.
- (c) change in internal energy of the cylinder.

(Given that Specific heat of cylinder= 400 J kg⁻¹ $^{\circ}C^{-1}$, Coefficient of volume expansion = 9 × 10⁻⁹ $^{\circ}C^{-1}$, Atmospheric pressure = 10⁹ N/m² and Density of cylinder = 9000 kg/m⁵)

$$\Rightarrow \Delta T = \frac{200005}{3 \text{kg} \times (4000)/\text{kg}^{0}\text{C})} = 50^{\circ}\text{C}$$

$$T_{\text{inst}} = 70^{\circ}\text{C}$$

(b) W = P_{2m}
$$\Delta V = P_{2m} V_0 \Lambda \Delta T$$

= $(10^2 \text{ N/m}^3) \left(\frac{1}{9 \times 10^3} \text{ m}^3\right) (9 \times 10^{-2} \text{ // C}) (50^{\circ} \text{ C}) = 0.05 \text{ J}$
(c) $\Delta U = \Delta Q - W = 20000 \text{ J} = 0.05 \text{ J} = 19999.95 \text{ J}$

- Q18. In a moving coil galvanometer, torque on the coil can be expressed as n = ki, where i is current through the wire and k is constant. The rectangular coil of the galvanometer having numbers of turns N, area A and moment of inertial is placed in magnetic field B. Find
 - (a) k in terms of given parameters N, I, A and B.
 - (b) the torsional constant of the spring, if a current is produces a deflection of m2 in the coll.
 - (c) the maximum angle through which coil is deflected, if charge Q is passed through the coll almost instantaneously (Ignore the damping in mechanical oscillations)
- Sol (a) T= iNAB sind
 - For a moving coll galvanometer o, = 90' ki = iNAB = k = NAB
 - (b) τ = Cθ

$$bNAB = C\pi 2 \Rightarrow C = \frac{2bNAB}{\pi}$$

(c) Angular impulse = h. dt = [NABidt = NABi2

Using energy of conservation

$$\frac{1}{2} \log_{D}^{2} - \frac{1}{2} C \theta_{max}^{2}$$

$$= \theta_{max} = \cos \sqrt{\frac{1}{C}} - C \sqrt{\frac{NAB\pi}{2}}$$