

## **Structure of Atom**

#### <u>SOL 1.</u>

Let the % of isotope with At. wt. 10.01 = x  $\therefore$  % of isotope with At. wt. 11.01 = (100 - x)At. wt. of boron = x \*10.01 + (100 - x) \*11.01/100 => 10.81 = x \*10.01 + (100 - x) \*11.01/100  $\therefore$  x = 20 Hence % of isotope with At. wt. 10.01 = 20% $\therefore$  % of isotope with At. wt. 11.01 = 100 - 20 = 80%.

#### <u>SOL 2.</u>

Elements usually have one or more isotopes and these isotopes have different atomic masses. So atomic weights are fractional number.

#### <u>SOL 3.</u>

TIPS/Formulae:  $\Delta E = E_3 - E_2 = hv = hc/\lambda \text{ or } \lambda = hc/E_3 - E_2$ Given  $E_2 = -5.42 * 10^{-12} \text{ erg}$   $E_3 = -2.41 * 10^{-12} \text{ erg}$  $\therefore 6.626 * 10^{-27} * 3 * 10^{10}/ -2.41 * 10^{-12} - (-5.42 * 10^{-12}) = 19.878 * 10^{-17}/3.01 * 10^{-12} = 6.604 * 10^{-5} \text{ cm} = 6.604 \text{ Å}$ 

#### <u>SOL 4.</u>

**TIPS/Formulae:** (i) Energy of n<sup>th</sup> orbit  $E_n = E_1/n^2$ (ii) Difference in energy  $= E_1 - E_2 = hv = hc/\lambda$  or  $\lambda = hc/E_1 - E_2$ Given  $E_1 = 2.17 * 10^{-11}$  $\therefore$  Energy of second orbit  $= E_2 = 2.17 * 10^{-11}/2^2 = 0.5425 * 10^{-11}$  erg  $\Delta = E_1 - E_2 = 2.17 * 10^{-11} - 0.5425 * 10^{-11} = 1.0275 * 10^{-11}$  erg  $\lambda = 6.62 * 10^{-27} * 3 * 10^{10}/1.6275 * 10^{-11} = 12.20 * 10^{-6}$  cm = **1220** Å

#### <u>SOL 5.</u>

To calculate the energy required to remove electron from atom,  $n = \infty$  is to be taken. Energy of an electron in nth orbit of hydrogen is given by  $E = 21.7 * 10^{-12} * 1/n^2 \text{ ergs}$   $\therefore \Delta E = 21.7 * 10^{-12} (1/2^2 - 1/\infty^2)$   $= -21.7 * 10^{-12} (1/4 - 0) = 21.7 * 10^{-12} * 1/4$   $= -5.42 * 10^{-12} \text{ ergs}$   $\therefore \Delta E = hc/\lambda$  ( $\because v = c/\lambda$ ) Or  $\lambda = hc/\Delta E$ Substituting the values,  $\lambda = 6.627 * 10^{-27} * 3 * 10^{10}/5.42 * 10^{-12}$  $= 3.67 * 10^{-5} \text{ cm}$ 



Ground state electronic configuration of Si

	Î		

3s

 $3p_x 3p_y 3p_z$ 

is in accordance with Hund's rule which states that electron pairing in any orbital (s, p, d or f) cannot take place until each orbital of the same sub-level contain 1 electron each of like spin.

## <u>SOL 7.</u>

For n = 3 and l = 2 (i.e., 3d orbital), the values of m varies from -2 to +2, -1, 0, +1, +2 and for each 'm' there are 2 values of 's', i.e.  $+\frac{1}{2}$  and  $-\frac{1}{2}$ .

 $\therefore$  Maximum no. of electrons in all the five d-orbitals is **10**.

#### <u>SOL 8.</u>

$$\begin{split} & E_n \text{ of } H = -21.76 \ ^*10^{-19}/n^2 \text{ J} \\ & \therefore E_n \text{ of } He^+ = -21.76 \ ^*10^{-19}/n^2 \ ^*Z^2 \text{ J} \\ & \therefore E_3 \text{ of } He^+ = -21.76 \ ^*10^{-19} \ ^*4/9 \text{ J} \end{split}$$

Hence energy equivalent to E<sub>3</sub> must be supplied to remove the electron from 3rd orbit of He<sup>+</sup>. Wavelength corresponding to this energy can be determined by applying the relation.  $E = hc/\lambda$ or  $\lambda = hc/E = 6.625 * 10^{-34} * 3 * / 10^8 * 9 / 21.76 * 10^{-19} * 4 = 2055 * 10^{-10} m = 2055 Å$ 

#### <u>SOL 9.</u>

TIPS/Formulae:  $\Delta E = RhcZ^2 (1/n_1^2 - 1/n_2^2)$ Here,  $R = 1.0967 * 10^7 m^{-1}$   $h = 6.626 * 10^{-34} J \text{ sec, } c = 3 * 10^8 m/\text{sec}$   $n_1 = 1, n_2 = 2 \text{ and for H-atom, } Z = 1$   $E_2 - E_1 = 1.0967 * 10^7 * 6.626 * 10^{-34} * 3 * 10^8 (1/1 - 1/4)$   $\Delta E = 1.0967 * 6.626 * 3 * 3/4 * 10^{-19} J$   $= 16.3512 * 10^{-19} J$   $= 16.3512 * 10^{-19}/1.6 * 10^{-19} \text{ eV} = 10.22 \text{ eV}$   $\Delta E = hc/\lambda = RhcZ^2 (1/n_1^2 - 1/n_2^2)$   $1/\lambda = RZ^2 (1/1 - 1/4) = RZ^2 * 3/4$ Given,  $\lambda = 3 * 10^{-8} = m$   $\therefore 1/3 * 10^{-8} = 1.0967 = Z^2 * 3/4 * 10^7$   $\therefore Z^2 = 10^8 * 4/3 * 3 * 1.0967 * 10^7 = 40/9 * 1.0967 = 4$  $\therefore Z = 2$ 

So it corresponds to He<sup>+</sup> which has 1 electron like hydrogen.



For He<sup>+</sup> ion, we have  $1/\lambda = Z^2 R_H [1/n_1^2 \cdot 1/n_2^2]$   $= (2)^2 R_H [1/(2)^2 - 1/(4)^2] = R_H 3/4 \dots(i)$ Now for hydrogen atom  $1/\lambda = R_H [1/n_1^2 \cdot 1/n_2^2] \dots(ii)$ Equating equation (i) and (ii), we get  $1/n_1^2 \cdot 1/n_2^2 = 3/4$ Obviously,  $n_1 = 1$  and  $n_2 = 2$ Hence, the transition  $\mathbf{n} = 2$  to  $\mathbf{n} = 1$  in hydrogen atom will have the same wavelength as the transition,  $\mathbf{n} = 4$  to  $\mathbf{n} = 2$  in He<sup>+</sup> species.

#### <u>SOL 11.</u>

**TIPS/Formulae:** Number of waves = n(n - 1)/2 where n = Principal quantum number or number of orbit number of waves = 3(3 - 1)/2 = 3 \* 2/2 = 3

#### **ALTERNATIVE SOLUTIONS:**

In general, the number of waves made by a Bohr electron in an orbit is equal to its quantum number.

According to Bohr's postulate of angular momentum, in the 3rd orbit

 $Mur = n h/2\pi$ 

Mur = 3 (h/2 $\pi$ ) .....(i) [n = 3]

According to de Broglie relationship

 $\lambda = h/mu$  ....(ii)

Substituting (ii) in (i), we get

 $(h/\lambda)$  r = 3  $(h/2\pi)$  or  $3\lambda = 2\pi r$ 

 $[\because mu = h/\lambda]$ 

Thus the circumference of the 3rd orbit is equal to 3 times the wavelength of electron i.e. the electron makes **three** revolution around the 3rd orbit.

#### ALTERNATIVE SOLUTION:

 $\begin{aligned} r_n & \text{ for } H = r_1 * n^2 \\ r_3 & \text{ for } H = 0.529 * 9 * 10^{-8} \text{ cm} \\ = .529 * 9 * 10^{-10} \text{ m} \quad (\because r_1 = 0.529 \text{ Å}) \\ \text{Also } u_n = Z \, u_1/n \text{ ;} \\ \therefore & u_3 = 2.19 * 10^8/3 \text{ cm sec}^{-1} = 2.19 * 10 + 16/3 \text{ m sec}^{-1} \\ (\because & u_1 = 2.19 * 10^8 \text{ cm sec}^{-1}) \\ \therefore & \text{ No. of waves in one round} \\ = 2\pi \, r_3/\lambda = 2\pi \, r_3/h/mv_3 = 2\pi \, r_3 * m/h \\ = 2 * 22 * 0.529 * 9 * 10^{-10} * 2.19 * 10^6 * 9.108 * 10^{-31}/7 * 3 * 6.62 * 10^{-34} = 3 \end{aligned}$ 

#### SOL 12.

Bond energy of I<sub>2</sub> 240kJ mol<sup>-1</sup> = 240 \* 10<sup>3</sup> J mol<sup>-1</sup> = 240 \*10<sup>3</sup>/6.023 \*10<sup>23</sup> J molecule<sup>-1</sup> = 3.984 \*10<sup>-19</sup> J molecule<sup>-1</sup> Energy absorbed =  $hc/\lambda = 6.626 *10^{-34}$  Js \*3 \*10<sup>8</sup> ms<sup>-1</sup>/4500 \*10<sup>-10</sup> m

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Kinetic energy = Absorbed energy – Bond energy  $\therefore$  Kinetic energy = 4.417 \*10<sup>-19</sup> – 3.984 \*10<sup>-19</sup> J = 4.33 \* 10<sup>-20</sup> J  $\therefore$  Kinetic energy of each atom of iodine

 $= 4.33 * 10^{-20}/2 = 2.165 * 10^{-20}$ 

## <u>SOL 13.</u>

The shortest wavelength transition in the Barlmer series corresponds to the transition  $n = 2 \rightarrow n = \infty$ . Hence,  $n_1 = 2$ ,  $n_2 = \infty$  Balmer  $\bar{v} = R_H \left(\frac{1}{n_1^2} - \frac{1}{n_2^2}\right) = (109677 \text{ cm}^{-1}) (1/2^2 - 1/\infty^2) = 27419.25 \text{ cm}^{-1}$ 

### <u>SOL 14.</u>

Work done while bringing an electron infinitely slowly from infinity to proton of radius  $a_0$  is given as follows

 $W = -e^2/4\pi\epsilon_0.a_0$ 

**NOTE :** This work done is equal to the total energy of an electron in its ground state in the hydrogen atom. At this stage, the electron is not moving and do not possess any K.E., so this total energy is equal to the potential energy.

T.E. = P.E + K.E. =  $e^2/4\pi\epsilon_0.a_0$  ....(i)

In order the electron to be captured by proton to form a ground state hydrogen atom it should also attain

K.E. =  $e^2/8\pi\epsilon_0 a_0$ 

(it is given that magnitude of K.E. is half the magnitude of P.E. Note that P.E. is –ve and K.E is +ve)

 $\begin{array}{l} \therefore \text{ T.E.} = \text{P.E} + \text{K.E.} = -\ e^2/4\pi\epsilon_0 a_0 + e^2/8\pi\epsilon_0 a_0 \\ \text{ or T.E.} = -\ e^2/8\pi\epsilon_0 a_0 \\ \text{P.E.} = 2 * \text{T.E.} = 2 * -e^2/8\pi\epsilon_0 a_0 \text{ or P.E.} = -e^2/8\pi\epsilon_0 a_0 \end{array}$ 

## <u>SOL 15.</u>

As the  $\propto$ -particle travelling with velocity, 'u', stops at a distance  $10^{-13}$  m, its K.E. becomes zero and gets converted into P.E.

 $\therefore 1/2 \text{ mu}^2 = 1/4\pi \epsilon_0 * 2\text{Ze}^2/\text{r or u}^2 = \text{Ze}^2/4\pi\epsilon_0 \text{ m.r}$ Here, Z = 29 for Cu atom => u<sup>2</sup> 29 \*(1.6 \*10<sup>-19</sup>)<sup>2</sup>/3.14 \*8.85 \*10<sup>-12</sup> \*(4 \*1.672 \*10<sup>-27</sup>) \*10<sup>-13</sup>  $\therefore$  u = 6.3 \* 10<sup>6</sup> m sec<sup>-1</sup>

## <u>SOL 16.</u>

 $1/2 \text{ mu}^2 = eV$ ; also  $\lambda = h/mu$  or  $u = h/m\lambda$   $\therefore 1/2 \text{ m} h^2/m^2 \lambda^2 = eV$  or  $V = 1/2 h^2/m\lambda^2 e$  $V = 1 * (6.62 * 10^{-34})^2/2 * 9.108 * 10^{-31} * (1.54 * 10^{-10})^2 * 1.602 * 10^{-19} = 63.3 \text{ volt}$ 

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Determination of number of moles of hydrogen gas,

N = PV/RT = 1 \* 1/0.082 \* 298 = 0.0409

The concerned reaction is  $H_2 \rightarrow 2H$  ;  $\Delta H = 436~kJ~mol^{-1}$ 

Energy required to bring 0.0409 moles of hydrogen gas to atomic state = 436 \* 0.0409 = 17.83 kJ

Calculate of total number of hydrogen atom in 0.0409 mole of  $H_2$  gas

1 mole of  $H_2$  gas has 6.02 \*  $10^{23}\,molecules$ 

0.0409 mole of H<sub>2</sub> gas =  $6.02 \times 10^{23}/1 \times 0.0409$  molecules

Since 1 molecule of H<sub>2</sub> gas has 2 hydrogen atoms  $6.02 * 10^{23} * 0.0409$  molecules of H<sub>2</sub> gas =  $2 * 6.02 * 10^{23} * 0.0409 = 4.92 * 10^{22}$  atoms of hydrogen since energy required to excite an electron from the ground state to the next excited state is given by

$$E = 13.6 \left(\frac{1}{n_1^2} - \frac{1}{n_2^2}\right) eV = 13.6 * (1/1 - 1/4) = 13.6 * 3/4 = 10.2 eV$$
$$= 1.632 * 10^{-21} kJ$$
Therefore energy required to quote 4.02 \* 10<sup>22</sup> electrons

Therefore energy required to excite  $4.92 * 10^{22}$  electrons =  $1.632 * 10^{-21} * 4.92 * 10^{22}$  kJ = 8.03 \* 10 = 80.3 kJ Therefore total energy required = 17.83 + 80.3 = 98.17 kJ

## <u>SOL 18.</u>

For maximum energy,  $n_1 = 1$  and  $n_2 = \infty$  $1/\lambda = R_H Z^2 \left(\frac{1}{n_1^2} - \frac{1}{n_2^2}\right)$ Since  $R_H$  is a constant and transition remains the same

 $1/\lambda \propto Z^2$ ;  $\lambda_{He}/\lambda_H = \frac{2_H^2}{2_{He}^2} = 1/4$ Hence,  $\lambda_{He} = 1/4 * 91.2 = 22.8$  nm

## <u>SOL 19.</u>

 $\Psi_{2s}^2$  = probability of finding electron within 2s sphere  $\Psi_{2s}^2$  = 0 (at node) (: Probability of finding an electron is zero at node)

 $\therefore 0 = 1/32\pi (1/a_0)^3 (2 - r_0/a_0)^2 \cdot e^{-\frac{2r_v}{a_0}}$ (Squaring the given value of  $\Psi_{2s}$ )
or  $[2 - r_0/a_0] = 0; \therefore 2 - r_0/a_0; 2a_0 = r_0$ 

#### <u>SOL 20.</u>

 $\lambda = h/mu = 6.627 * 10^{-34}/0.1 * 100$ or  $\lambda = 6.627 * 10^{-35} m = 6.627 * 10^{-25} Å$ 

## <u>SOL 21.</u>

For hydrogen atom, Z = 1, n = 1 V = 2.18 \*  $10^6$  \* Z/n ms<sup>-1</sup> = 2.18 \*  $10^6$  ms<sup>-1</sup> de Broglie wavelength,

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