

CHAPTER -6 The Triangle and its Properties | CLASS 7TH

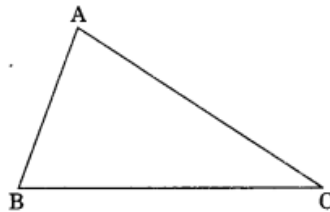
MATHS IMPORTANT QUESTIONS

Important Questions

Question 1.

In $\triangle ABC$, write the following:

- Angle opposite to side BC.
- The side opposite to $\angle ABC$.
- Vertex opposite to side AC.

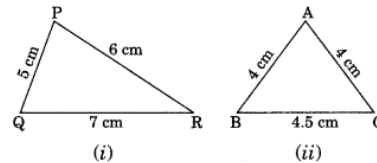


Solution:

- In $\triangle ABC$, Angle opposite to BC is $\angle BAC$
- Side opposite to $\angle ABC$ is AC
- Vertex opposite to side AC is B

Question 2.

Classify the following triangle on the bases of sides



Solution:

- $PQ = 5$ cm, $PR = 6$ cm and $QR = 7$ cm

$$PQ \neq PR \neq QR$$

Thus, $\triangle PQR$ is a scalene triangle.

- $AB = 4$ cm, $AC = 4$ cm

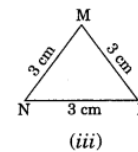
$$AB = AC$$

Thus, $\triangle ABC$ is an isosceles triangle.

- $MN = 3$ cm, $ML = 3$ cm and $NL = 3$ cm

$$MN = ML = NL$$

Thus, $\triangle MNL$ is an equilateral triangle.



Question 3.

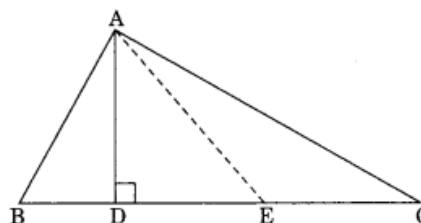
In the given figure, name the median and the altitude. Here E is the midpoint of BC.

Solution

In $\triangle ABC$, we have

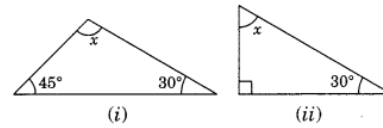
AD is the altitude.

AE is the median.



Question 4.

In the given diagrams, find the value of x in each case.



Solution:

(i) $x + 45^\circ + 30^\circ = 180^\circ$ (Angle sum property of a triangle)

$$\Rightarrow x + 75^\circ = 180^\circ$$

$$\Rightarrow x = 180^\circ - 75^\circ$$

$$x = 105^\circ$$

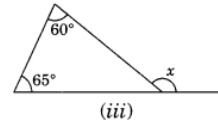
(ii) Here, the given triangle is right angled triangle.

$$x + 30^\circ = 90^\circ$$

$$\Rightarrow x = 90^\circ - 30^\circ = 60^\circ$$

(iii) $x = 60^\circ + 65^\circ$ (Exterior angle of a triangle is equal to the sum of interior opposite angles)

$$\Rightarrow x = 125^\circ$$



Question 5.

Which of the following cannot be the sides of a triangle?

(i) 4.5 cm, 3.5 cm, 6.4 cm

(ii) 2.5 cm, 3.5 cm, 6.0 cm

(iii) 2.5 cm, 4.2 cm, 8 cm

Solution:

(i) Given sides are, 4.5 cm, 3.5 cm, 6.4 cm

$$\text{Sum of any two sides} = 4.5 \text{ cm} + 3.5 \text{ cm} = 8 \text{ cm}$$

Since $8 \text{ cm} > 6.4 \text{ cm}$ (Triangle inequality)

The given sides form a triangle.

(ii) Given sides are 2.5 cm, 3.5 cm, 6.0 cm

$$\text{Sum of any two sides} = 2.5 \text{ cm} + 3.5 \text{ cm} = 6.0 \text{ cm}$$

Since $6.0 \text{ cm} = 6.0 \text{ cm}$

The given sides do not form a triangle.

(iii) 2.5 cm, 4.2 cm, 8 cm

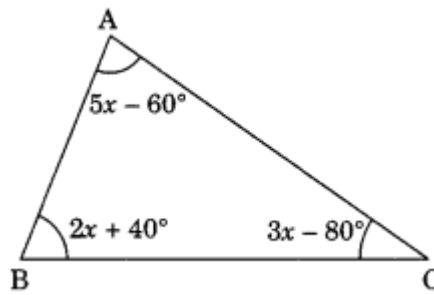
$$\text{Sum of any two sides} = 2.5 \text{ cm} + 4.2 \text{ cm} = 6.7 \text{ cm}$$

Since $6.7 \text{ cm} < 8 \text{ cm}$

The given sides do not form a triangle.

Question 6.

In the given figure, find x .



Solution:

In $\triangle ABC$, we have

$5x - 60^\circ + 2x + 40^\circ + 3x - 80^\circ = 180^\circ$ (Angle sum property of a triangle)

$$\Rightarrow 5x + 2x + 3x - 60^\circ + 40^\circ - 80^\circ = 180^\circ$$

$$\Rightarrow 10x - 100^\circ = 180^\circ$$

$$\Rightarrow 10x = 180^\circ + 100^\circ$$

$$\Rightarrow 10x = 280^\circ$$

$$\Rightarrow x = 28^\circ$$

Thus, $x = 28^\circ$

Question 7.

One of the equal angles of an isosceles triangle is 50° . Find all the angles of this triangle.

Solution:

Let the third angle be x° .

$$x + 50^\circ + 50^\circ = 180^\circ$$

$$\Rightarrow x^\circ + 100^\circ = 180^\circ$$

$$\Rightarrow x^\circ = 180^\circ - 100^\circ = 80^\circ$$

Thus $\angle x = 80^\circ$

Question 8.

In $\triangle ABC$, $AC = BC$ and $\angle C = 110^\circ$. Find $\angle A$ and $\angle B$.

Solution:

In given $\triangle ABC$, $\angle C = 110^\circ$

Let $\angle A = \angle B = x^\circ$ (Angle opposite to equal sides of a triangle are equal)

$$x + x + 110^\circ = 180^\circ$$

$$\Rightarrow 2x + 110^\circ = 180^\circ$$

$$\Rightarrow 2x = 180^\circ - 110^\circ$$

$$\Rightarrow 2x = 70^\circ$$

$$\Rightarrow x = 35^\circ$$

Thus, $\angle A = \angle B = 35^\circ$

